



# *BSSM 50<sup>th</sup> Anniversary*

University of South Carolina

## **Image-based Measurements in Solid Mechanics: A Brief History, Static and Dynamic Application Examples and Recent Developments**



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# Outline

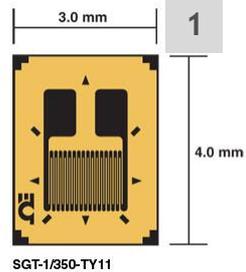
- **Brief History**
  - *Measurement Methods*
  - *Digital Image Correlation*
- **Digital Image Correlation Methods**
  - *2D-DIC*
    - *Early Applications*
  - *3D-DIC*
    - *Early Applications*
  - *V-DIC*
    - *Applications*
- **3D-DIC Applications and Details**
  - *Composite Materials in Bending-Compression*
  - *Shingles in 340 km/h winds*
- **The Future**
  - *Integration with Design and Development*
  - *Future Trends in Digital Image Based Methods*
- **Acknowledgements**
  - Sponsors and students who did the work





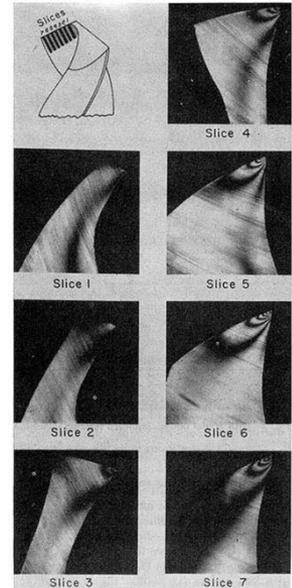
# Brief History: Measurement Methods

- In the mid 20<sup>th</sup> century, experimental methods in solid mechanics focused on point-wise measurements for quantitative data



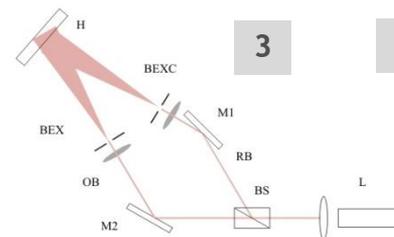
- Early full-field measurements were made in photo-elastic, polymeric materials
  - Through-thickness average effects
  - Local effects using a complex method known as “stress-freezing”

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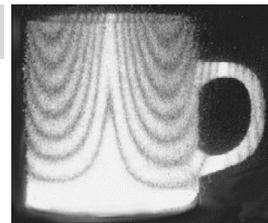
- The advent of lasers and interferometry methods circa 1960s provided investigators with new full-field measurement capability.

- Recording was via film media



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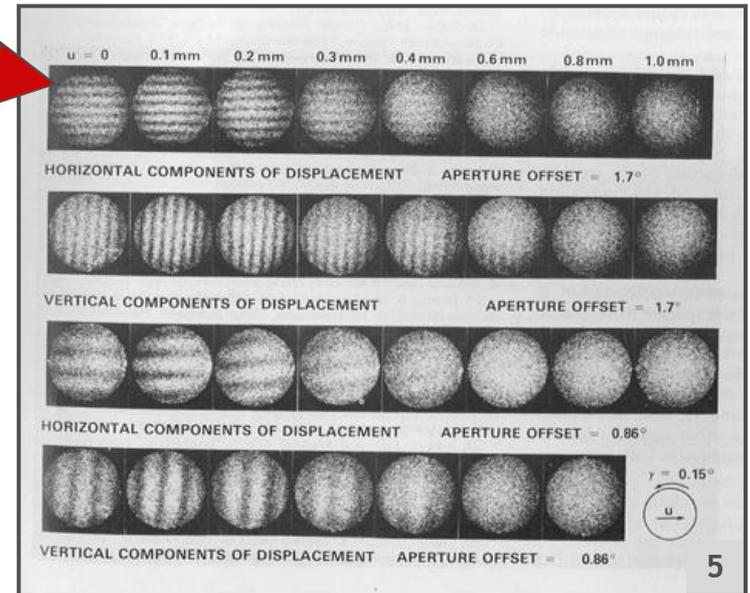
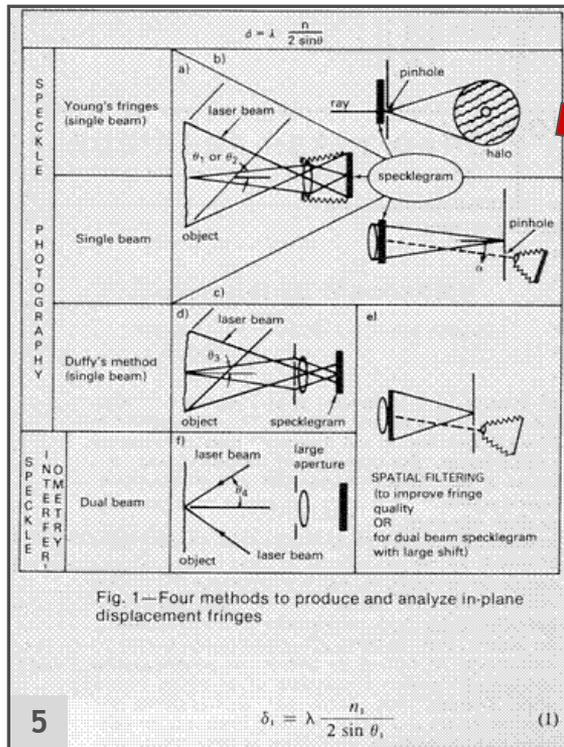
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# Brief History: Measurement Methods

- Vincent J. Parks, 1980
  - Experimentally showed that the range of displacement measurements that was possible using speckle photography was limited due to de-correlation.



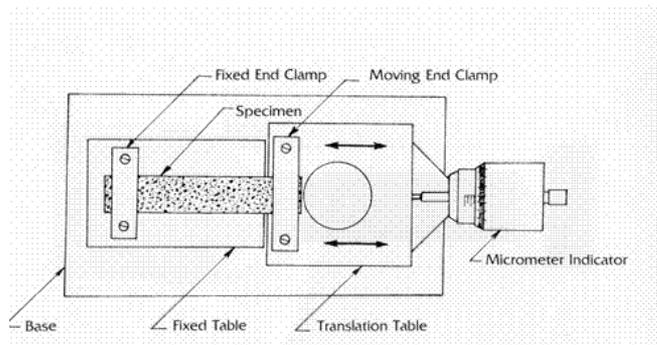
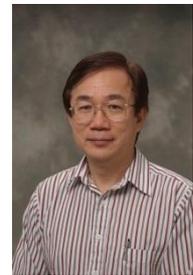
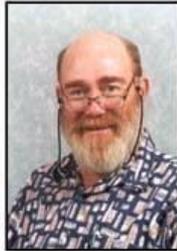
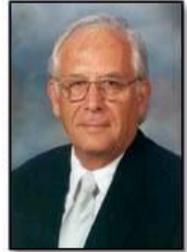
$$\delta_s = \lambda \frac{n_s}{2 \sin \theta_s} \quad (1)$$





# Brief History: Digital Image Correlation

- **1980, William F. Ranson and Walter H. Peters III**
  - For 2D, through-thickness averaged, ultra-sound applications, proposed approach for conversion of digitized ultra-sound images into estimates for local surface displacements by employing continuum-based matching principles
- **1982, Cheng and Sutton; Sutton and Wolters**
  - Developed non-linear least squares approaches using first-order gradients in a matching function to obtain local displacements.
- **1985, TC Chu et al**
  - Using a DAGE MTI analog camera to record images of a speckle pattern at 8 bits, demonstrating conclusively that the method could be used to measure deformations
    - Translations, large or small
    - Rotations, large or small
    - Strains, large and relatively small



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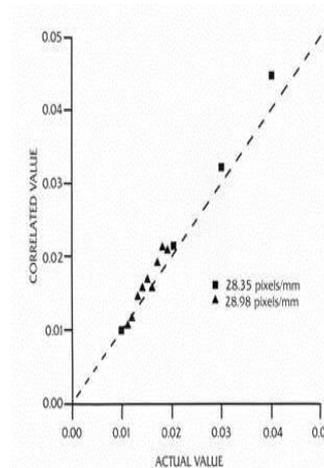


Figure 24  
Correlated Data for Finite Strain Test





# Brief History: Digital Image Correlation

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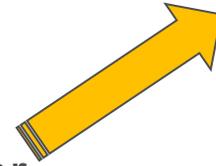
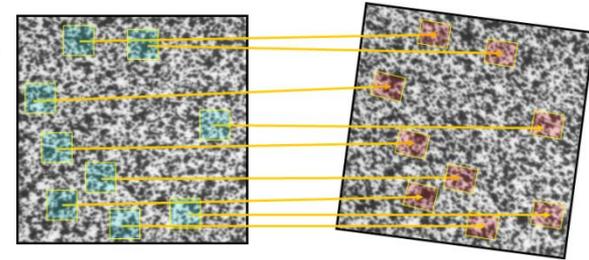
- **1989, Bruck et al**
  - Developed and demonstrated order of magnitude speed improvement using Hessian-based methodology for computing iterative improvements in optimal matching positions of subsets
  - Used linear shape functions for subset-based matching
- **1993, Luo, Chao et al**
  - Developed a stereo-vision system and verified the ability to make local strain and deformation measurements in cracked material
- **1996, Helm, McNeill et al**
  - Developed a robust stereo-vision system and demonstrated used on full-scale aero-structures as well as on laboratory-scale specimens
- **2000, Bay et al**
  - Extended 2D and 3D methods to volumetric images and performs digital image correlation on volumetric elements on the interior of a material
  - Limited to those materials providing sufficient contrast during tomographic imaging
  - Requires a tomographic imaging facility





# Brief History: Digital Image Correlation

- The rapid growth of **computer technology** that spurred continued growth of computational methods also provided the foundation for the explosion of growth in vision-based full-field experimental measurement method
  - 2D-DIC for SEM, AFM and planar loading and surfaces
  - 3D-DIC for general motion and deformation of curved or planar surfaces
  - V-DIC or Digital Volume Correlation for interior deformation measurements in opaque solids
- Today, the methods are used worldwide by scientists and investigators seeking to obtain full-field quantitative measurement of motions and deformations.

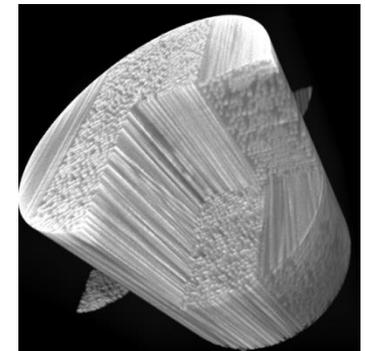


12, 13



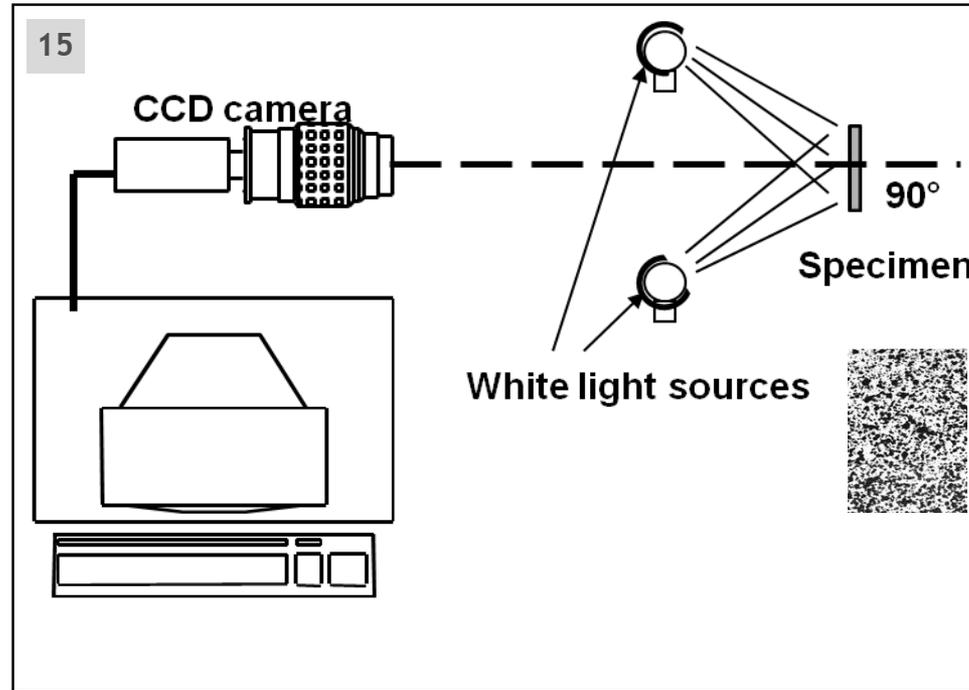
□ X-Radia Micro-CT

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# 2D Image Correlation: Basic Concepts



Single CCD camera positioned perpendicular to object surface.

- Specimen has a random pattern on its surface
- Uniform illumination is provided by white light sources
- Loading nominally in-plane, minimizing out of plane motion





# 2D Image Correlation: Basic Concepts

## General Remarks

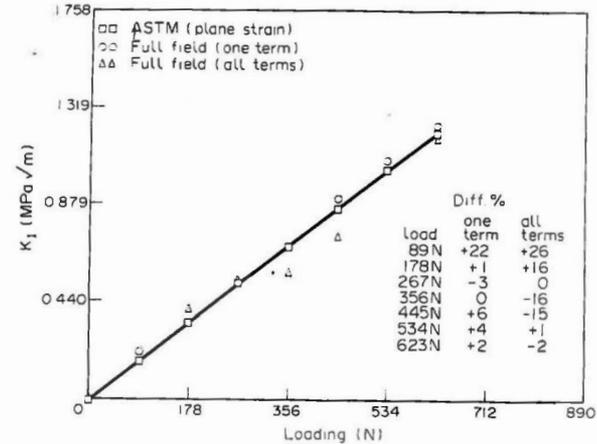
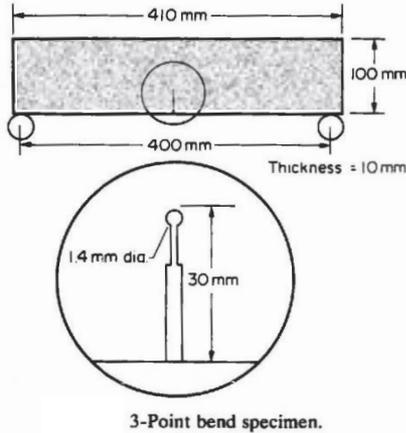
- Relatively simple to use under both laboratory and field conditions
- Relatively simple pattern application for many applications
  - Not so simple for microscale applications
- Data acquisition and data analysis procedures are well established
- Successfully used to make measurements on a range of specimen sizes from 0.01 mm to 2m
- Near real time analysis, with data analyzed at > 15000 subsets per second
- Accuracy nominally unaffected by large in-plane rotations or translations
  - Strain levels over 300% have been successfully measured
- Variability less than 0.01 pixels in displacement on a point-to-point basis are commonly obtained
- Accuracy of 100  $\mu$ s or smaller in strain on a point-to-point basis through differentiation of smoothed displacement data.
- Effect of out-of-plane displacement is readily estimated and minimized using equation  $w/Z$ , where  $w$  is out-of-plane motion and  $Z$  is distance from specimen to camera



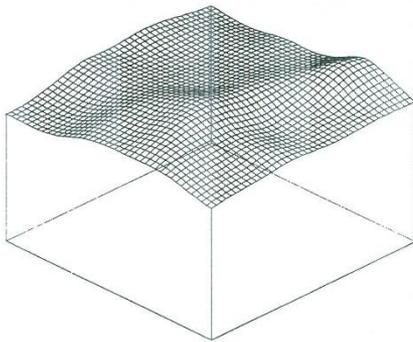


# 2D Image Correlation: Key Developments

- First LEFM measurements with DIC (1985-1987)



- Improving and speeding up DIC; differential corrections for efficient DIC (1987-1989)



$$S(x, y, u, v, \frac{\partial u}{\partial x}, \frac{\partial u}{\partial y}, \frac{\partial v}{\partial x}, \frac{\partial v}{\partial y}) = \frac{\Sigma [F(x, y) * G(x^*, y^*)]}{[\Sigma (F(x, y)^2) * \Sigma (G(x^*, y^*)^2)]}$$

$$x^* = x + u + \frac{\partial u}{\partial x} \Delta x + \frac{\partial u}{\partial y} \Delta y$$

$$y^* = y + v + \frac{\partial v}{\partial x} \Delta x + \frac{\partial v}{\partial y} \Delta y$$

$$P_i = \begin{pmatrix} u \\ v \\ \frac{\partial u}{\partial x} \\ \frac{\partial u}{\partial y} \\ \frac{\partial v}{\partial x} \\ \frac{\partial v}{\partial y} \end{pmatrix}$$

$$\nabla(P_i) = \begin{pmatrix} \frac{\partial S}{\partial u} \\ \frac{\partial S}{\partial v} \\ \frac{\partial S}{\partial (\frac{\partial u}{\partial x})} \\ \frac{\partial S}{\partial (\frac{\partial u}{\partial y})} \\ \frac{\partial S}{\partial (\frac{\partial v}{\partial x})} \\ \frac{\partial S}{\partial (\frac{\partial v}{\partial y})} \end{pmatrix}$$

$$H_{ij} = [\partial^2 S / \partial P_i \partial P_j]$$

TABLE 1—AVERAGE CPU TIME\* (IN SECONDS) per subset

Test Performed	Bicubic		Column	
	50 x 50 Subsets	20 x 20 Subsets	50 x 50 Subsets	20 x 20 Subsets
Translation	20.72	5.95	54.21	8.28
Rotation	55.36	6.63	n/a	n/a

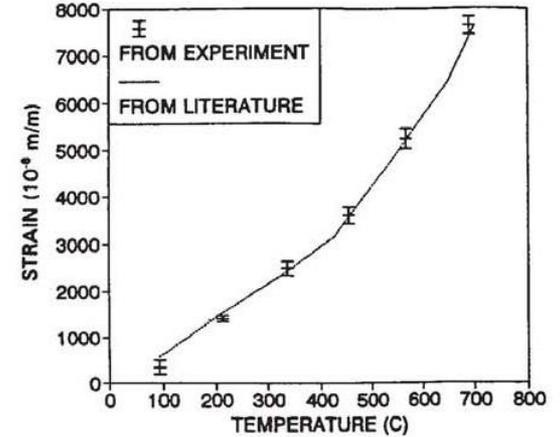
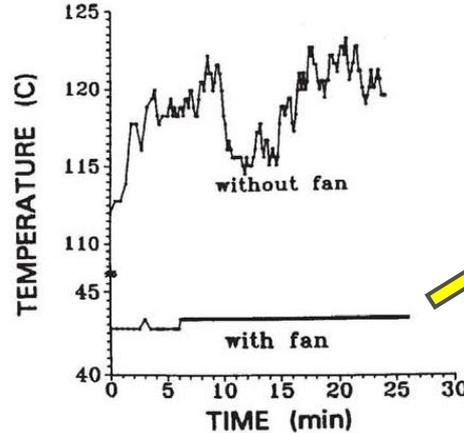
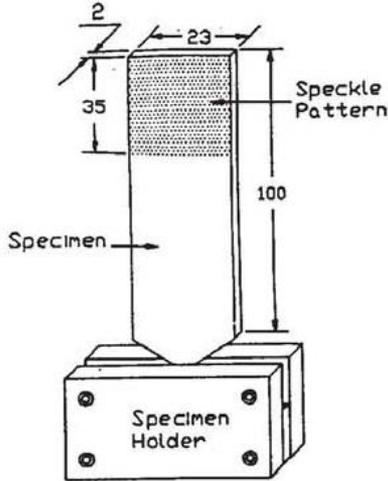
\*For a Vax 11/780 minicomputer

$$\Delta P_i = -H^{-1}(P_i) * \nabla(P_i)$$

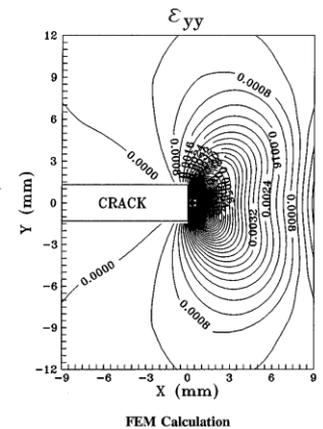
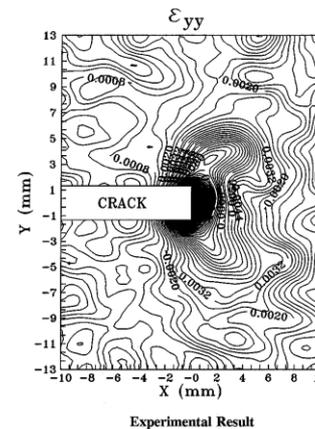
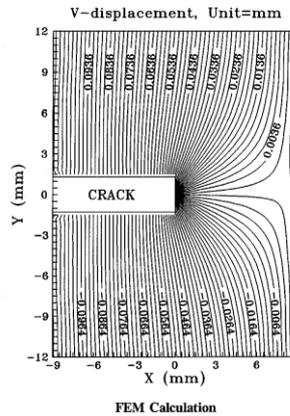
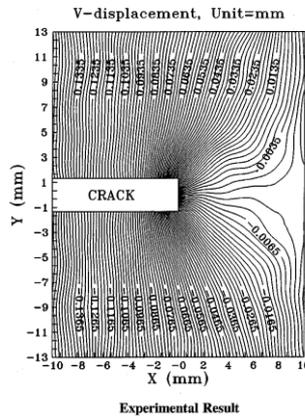
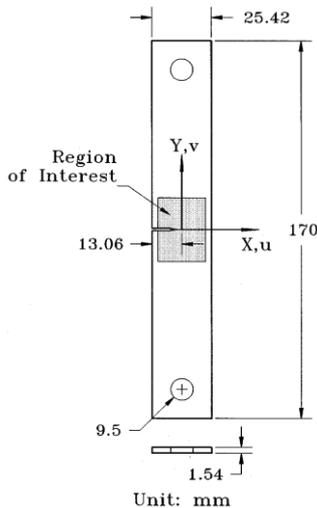


# 2D Image Correlation: Key Developments

- First high temperature measurements with DIC (1994-1996)



- First long-duration creep fracture w/DIC measurements. IN800 at 650°C for 147 hrs in lab air. Ceramic paint and pattern (1995-1998).

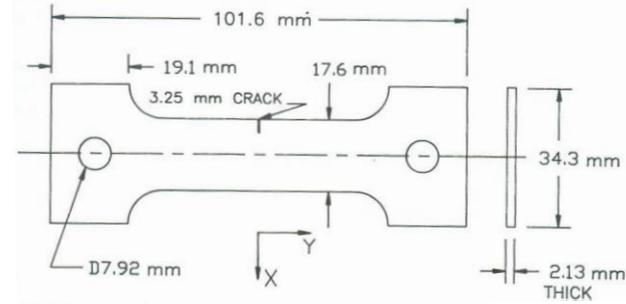
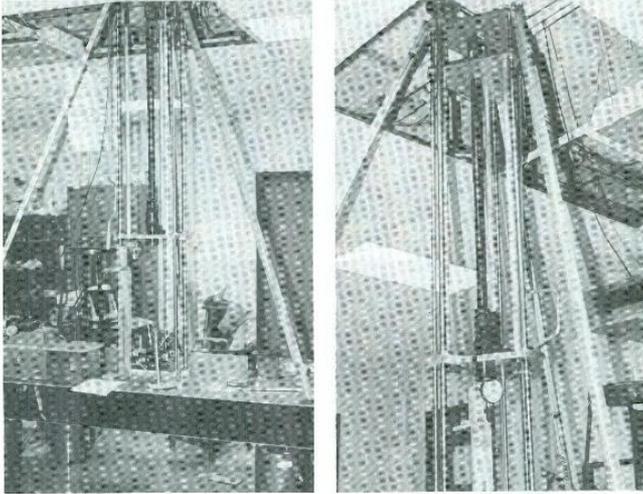




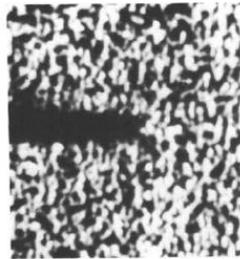
# 2D Image Correlation: Key Developments

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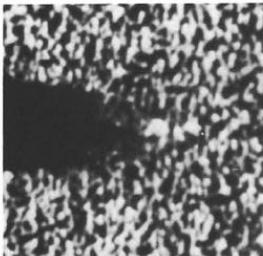
- Ductile fracture at high mag.(1990-1994)



$\Delta a = 0.00$  mm



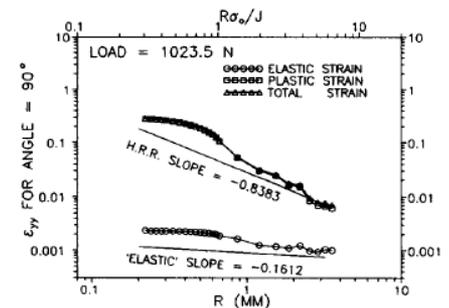
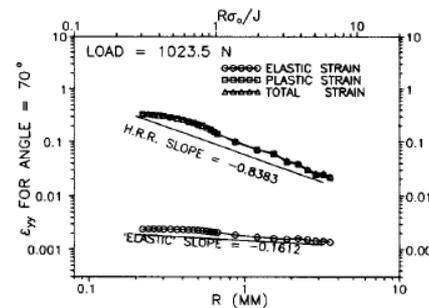
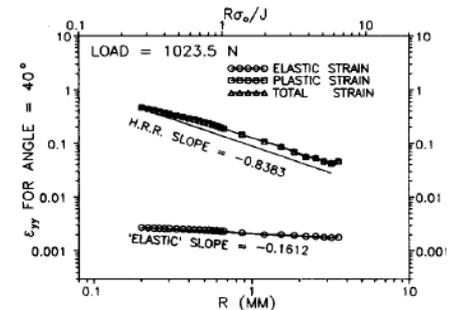
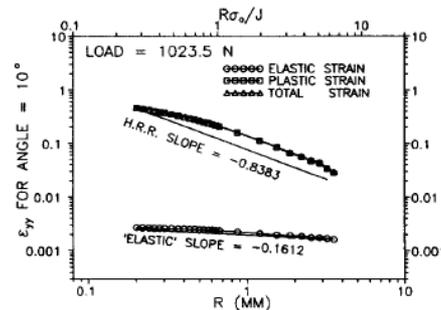
$\Delta a = 0.00$  mm



$\Delta a = 0.67$  mm



$\Delta a = 0.82$  mm



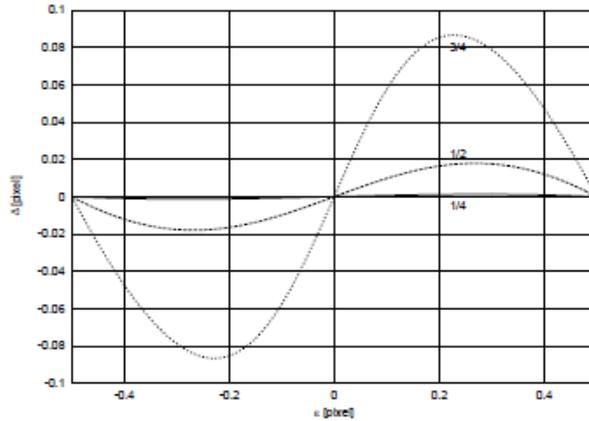


# 2D Image Correlation: Key Developments

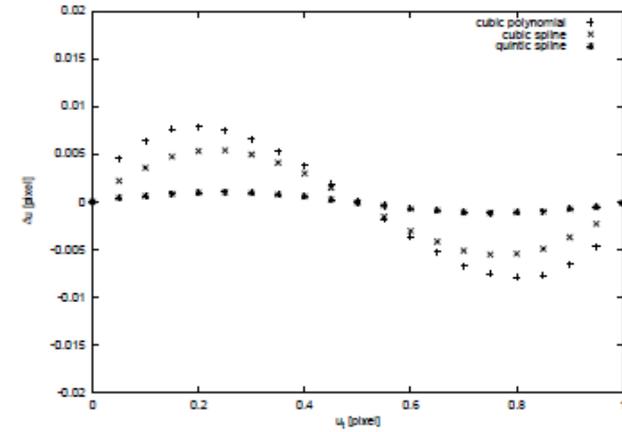
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- First two papers providing theoretical error predictions for 2D DIC
- INTERPOLATION INDUCED BIAS (1998-2000)

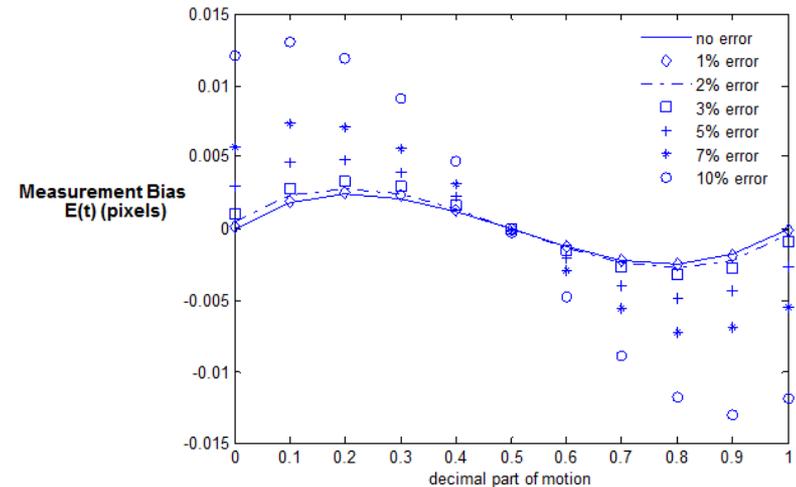
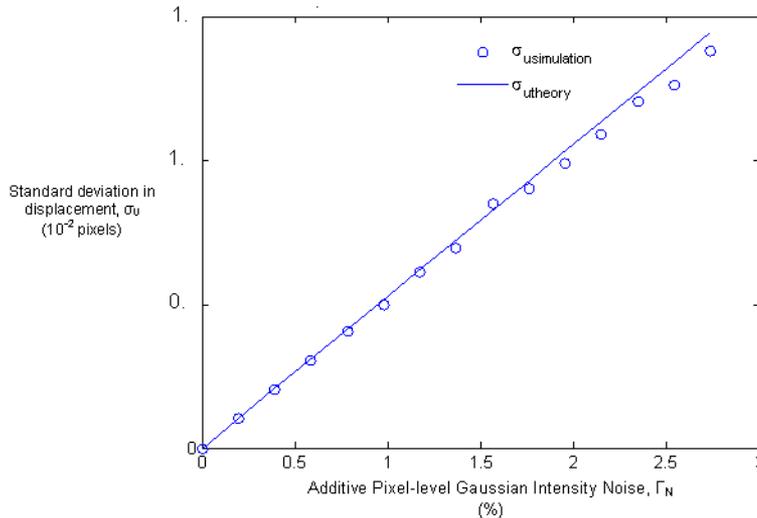
## THEORY (cubic polynomial)



## SIMULATIONS



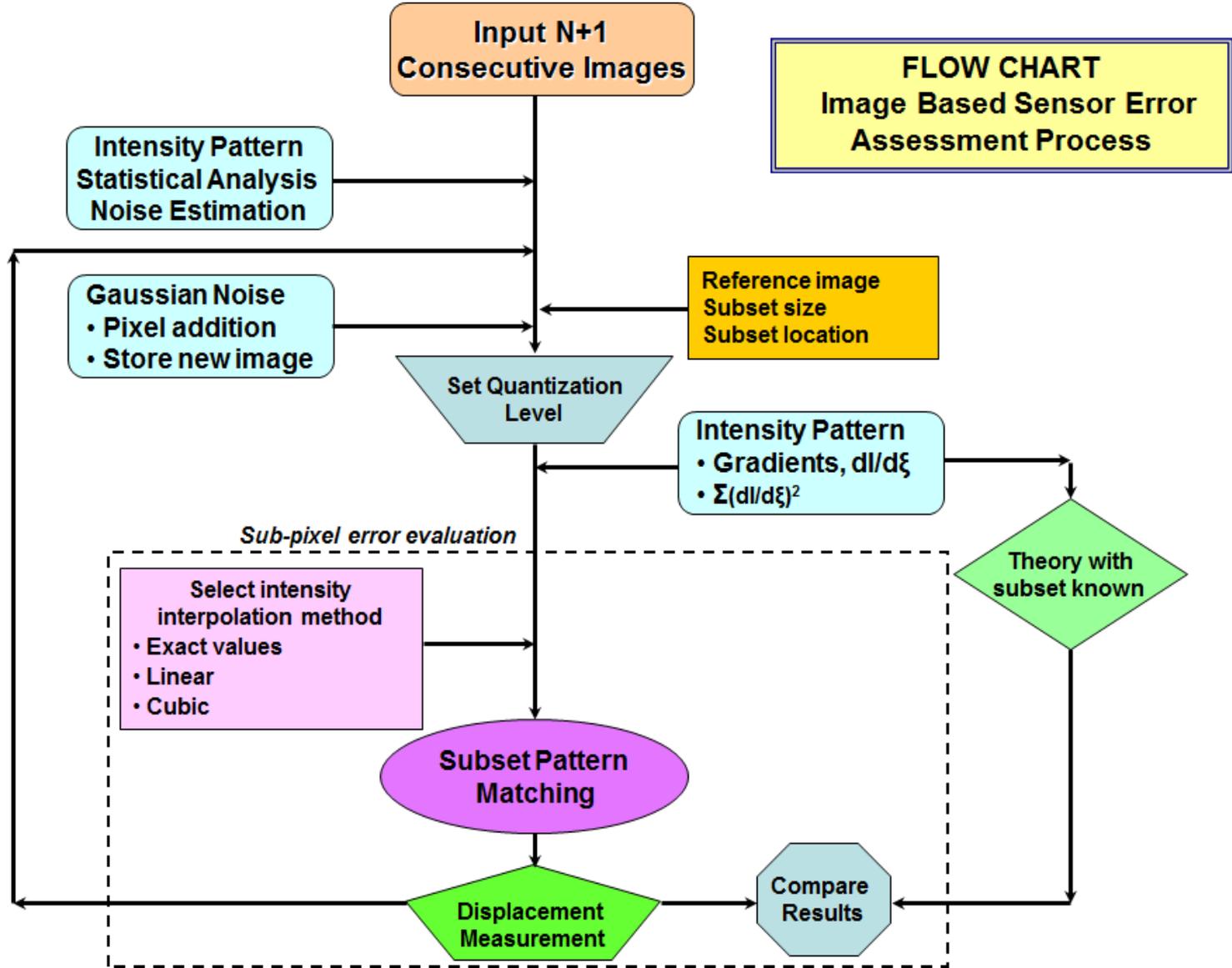
- VARIANCE AND NOISE-INDUCED BIAS (2005-2009)





# 2D Image Correlation: Key Developments

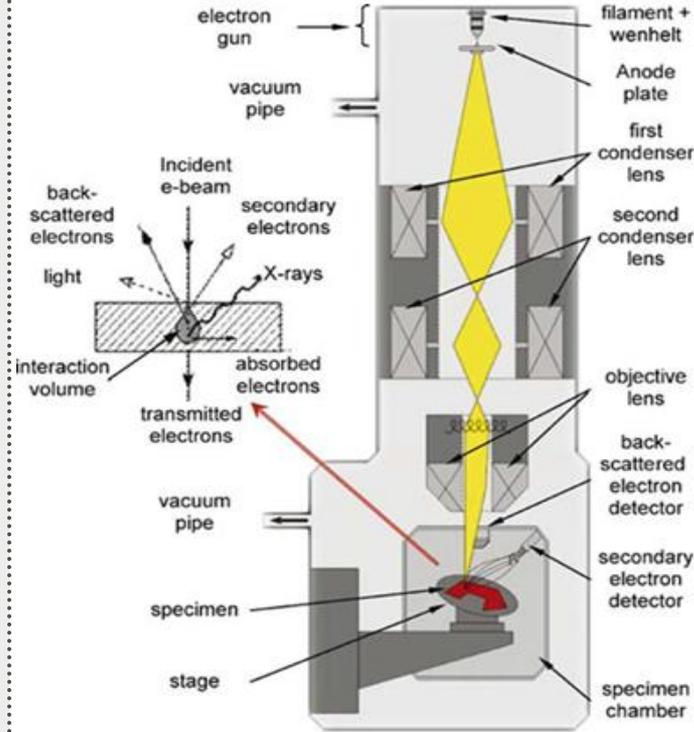
- Simulation process for each sub-pixel translation.



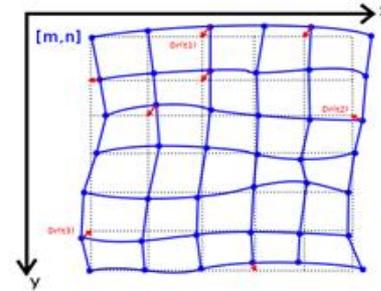


# 2D Image Correlation: Key Developments

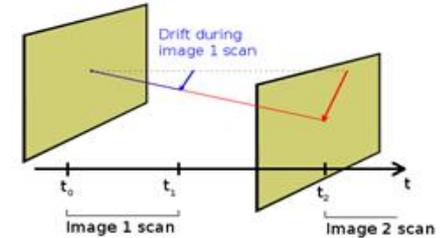
## SEM DIC with distortion corrections (2003)



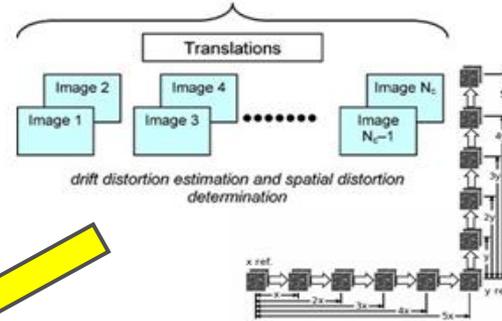
(1) Spatial distortion in an SEM which varies from experiment to experiment



(2) Drift distortion which is non-linear and varies over time



### Calibration Phase



### Measurement Phase

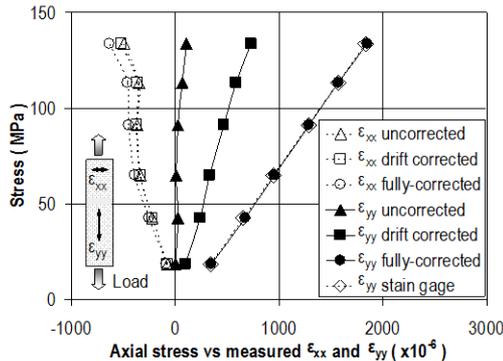
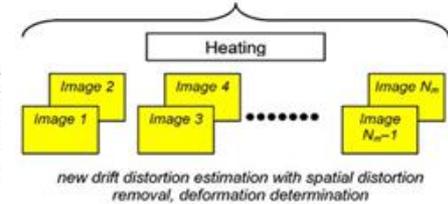
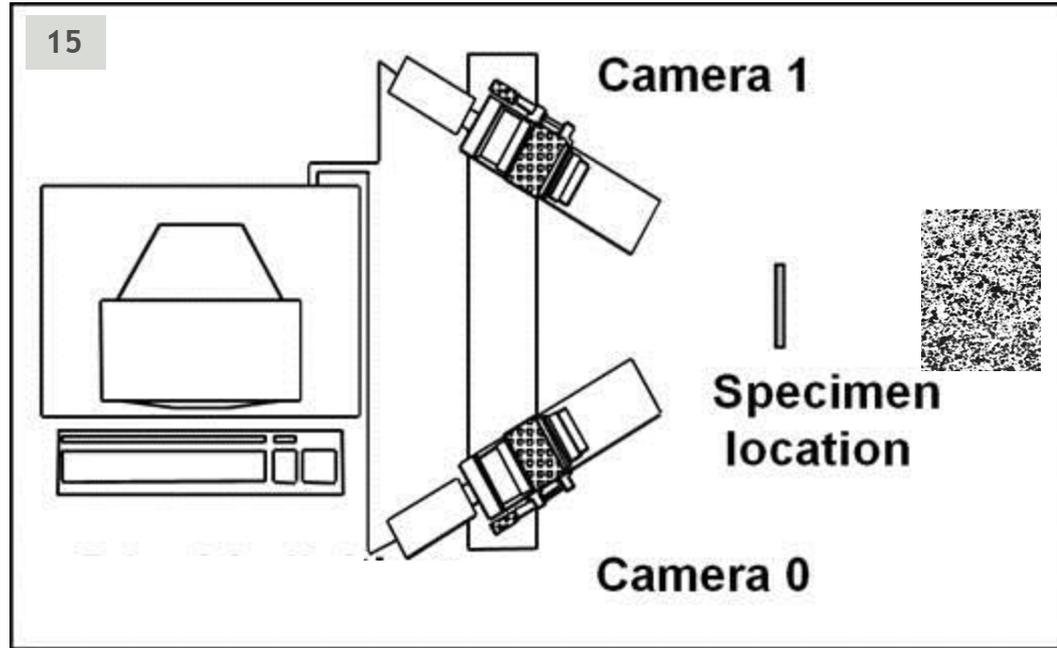


Fig. 9. Uniaxial stress versus axial strain and transverse strain for uncorrected, drift corrected and fully corrected image correlation data.



# 3D Image Correlation: Basic Concepts



- Two or more CCD cameras positioned to view same object area
- Specimen has a random pattern on its surface
  - Uniform illumination is provided by white light sources
  - General loading of specimen is allowed, while maintaining images of same object region in at least two cameras
  - Images acquired simultaneously by all cameras





# 3D Image Correlation: Basic Concepts

## General Remarks

- Full, three-dimensional displacement measurements obtained in laboratory and field conditions
- Calibration of camera system is required to convert image motions into accurate 3D measurements
  - Initial shape and 3D displacements are measured
- Data acquisition and data analysis procedures are well established
- Curved or planar objects from 0.50 mm to several meters in size
- Includes effect of perspective in image analysis
- High speed data analysis with data analyzed at > 3000 subset pairs per second
- Accuracy unaffected by large rotations or translations
  - Out-of-plane motion is measured, so does not affect accuracy of the in-plane measurements
- Accuracy of 3D displacement data is a function of camera system and camera noise level
  - Both variance and bias equations are available for estimating displacement errors
- Accuracy of 100  $\mu\text{s}$  or smaller in strain on a point-to-point basis through differentiation of smoothed displacement data.





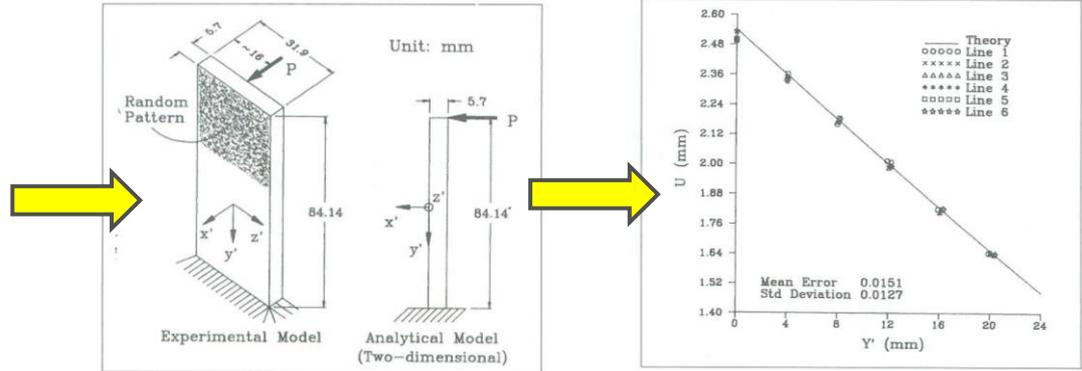
# 2D Image Correlation: Key Developments

## Early 3D vision system and 3D-DIC (1990-1994)

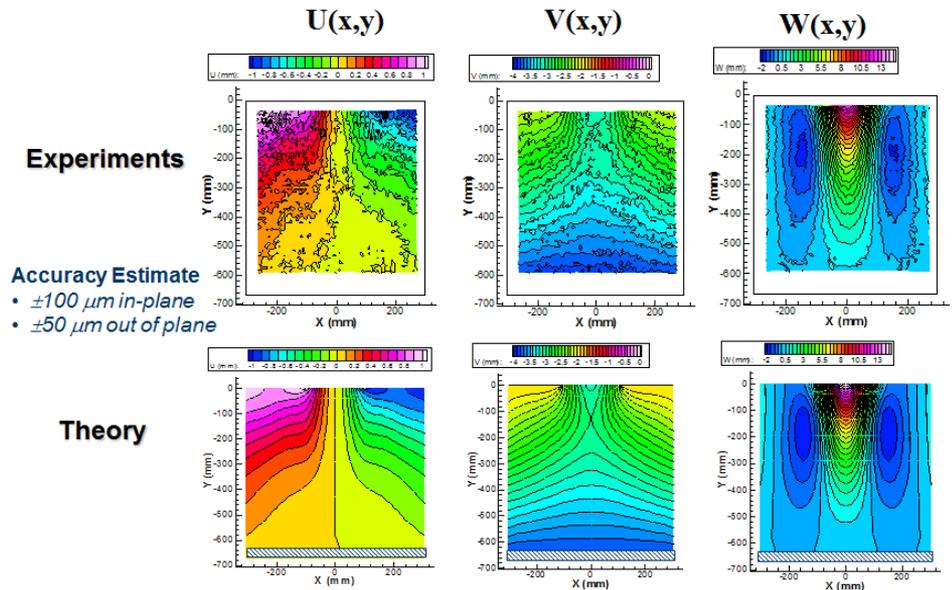
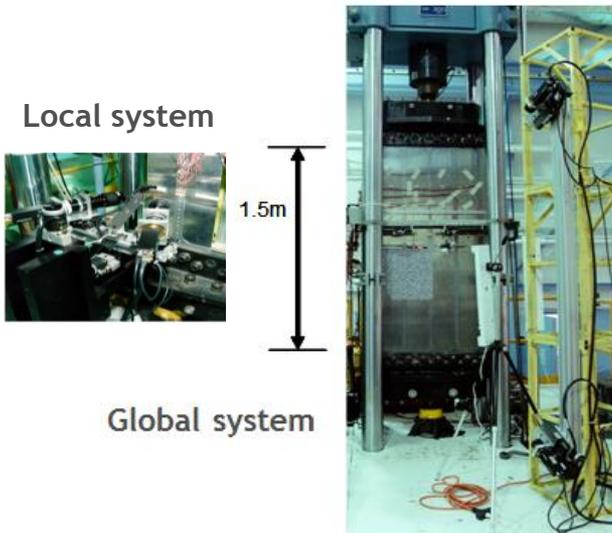
TABLE 1—CALIBRATION POINT LOCATIONS IN REFERENCE COORDINATE SYSTEM AND IMAGE POINT LOCATIONS IN COMPUTER-IMAGE COORDINATE SYSTEM COR,  $\rho = 20$  DEG

Point No.	Calibration Points			Image Points at Camera #1				Image Points at Camera #2			
	X (mm)	Y (mm)	Z (mm)	V (pixel)	H (pixel)	V (pixel)	H (pixel)	V (pixel)	H (pixel)		
1	0.00	0.00	0.00	267.00	240.00	290.73	262.95				
2	3.00	0.00	0.00	281.30	239.93	276.66	262.80				
3	-3.00	0.00	0.00	252.96	240.15	304.56	262.89				
4	-3.00	5.00	4.00	318.53	173.00	370.09	196.09				
5	0.00	5.00	4.00	333.14	172.18	356.79	196.24				
6	3.00	5.00	-4.00	348.03	308.57	342.93	331.02				
7	-3.00	5.00	-4.00	318.39	307.80	369.80	330.13				
8	-3.00	-5.00	-4.00	186.37	308.26	239.65	329.15				
9	0.00	-5.00	-4.00	200.00	308.71	225.22	329.59				
10	3.00	-5.00	-4.00	213.98	309.00	210.76	330.05				
11	3.00	-5.00	4.00	214.00	170.38	211.01	195.01				
12	0.00	-5.00	4.00	200.12	171.22	225.80	195.79				
13	-3.00	-5.00	4.00	186.55	172.67	240.04	196.42				
14	-3.00	-10.00	8.00	119.12	102.72	176.13	130.68				
15	0.00	-10.00	8.00	132.28	101.30	161.25	129.32				
16	3.00	-10.00	8.00	145.70	99.97	146.13	128.01				
17	3.00	10.00	8.00	414.47	103.36	410.94	125.51				
18	0.00	10.00	8.00	368.99	104.94	423.94	126.90				
19	-3.00	10.00	8.00	363.76	106.24	436.79	128.09				
20	-3.00	10.00	-8.00	383.49	375.00	436.34	398.63				
21	0.00	10.00	-8.00	398.86	376.01	423.41	399.82				
22	3.00	10.00	-8.00	414.25	377.04	410.21	400.99				
23	3.00	-10.00	-8.00	145.35	379.50	145.06	387.24				
24	0.00	-10.00	-8.00	132.00	378.44	160.25	386.12				
25	-3.00	-10.00	-8.00	118.83	377.37	175.13	395.00				

Note: The accuracy of calibration points is 0.001 mm; The accuracy of image points is 0.05 pixels.



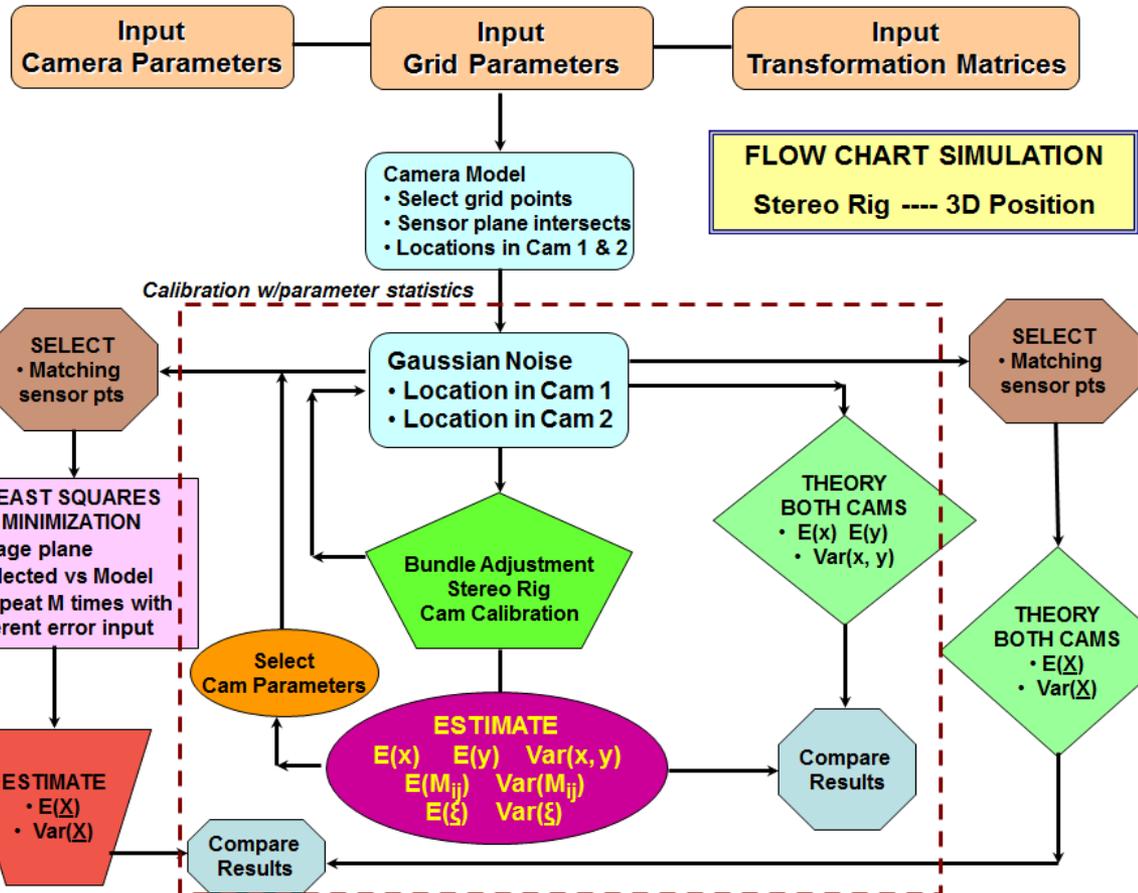
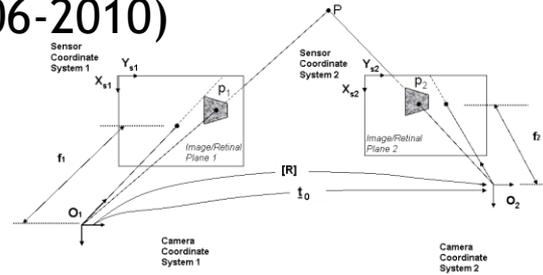
## Improving 3D-DIC systems for field studies. Aero-structures (1996-2003)





# 2D Image Correlation: Key Developments

## □ Error Propagation in 3D DIC (2006-2010)

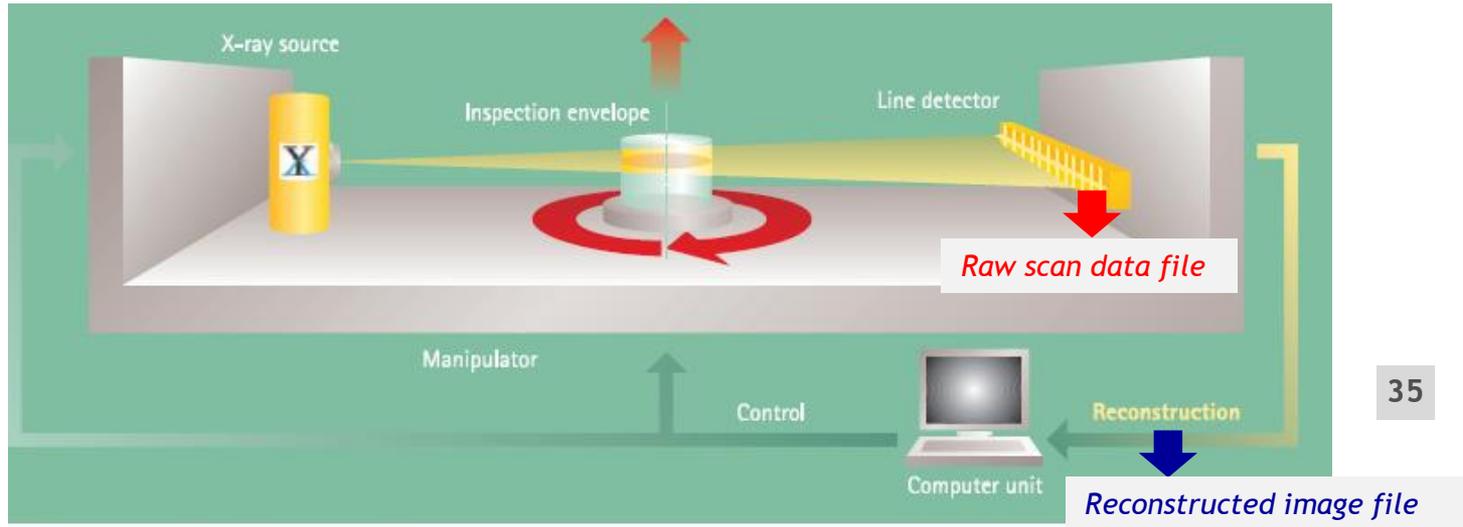


(x,y) = sensor position of a grid pt.  
 $M_{ij}$  = matrix from sensor to 3D location  
 $\xi$  = vector of 26 camera parameters used in M matrix





# Volumetric DIC: Basic Concepts



CT inspection using line detector

- System shown uses fan beam scanning approach
- Raw scan data file is digitally stored for each line and rotation angle
- Data is transferred to algorithms embedded in CT system and used to reconstruct images for each loading state
- Image data for each loading state used with optimization algorithms to determine internal deformations





# Volumetric DIC: Basic Concepts

## General Remarks

- Requires volumetric imaging system
- Pattern generally comes from natural internal sources, unless seeding of material is viable
  - When seeding material to improve pattern, may affect material response
- Image acquisition is slow, with lab CT images requiring up to several hours to complete high resolution scanning
- Noise levels are relatively high, with 3% noise or higher common in CT systems
- Data acquisition and image reconstruction procedures are well established, though prone to introduce artifacts
  - Image artifacts commonly seen in volumetric images can reduce accuracy of the matching process.
- Images can be obtained for small and large specimens
- Images are large, requiring efficient memory management and fast matching algorithms to reduce analysis time
- Accuracy nominally unaffected by large rotations or translations
  - Requires robust “initial guess” methods for estimating local motions
- Accuracy of  $\pm 0.02$  voxels in displacement on a point-to-point basis have been obtained in recent CT studies with high contrast patterns





# 2D Image Correlation: Key Developments

- First volumetric DIC Paper (BK Bay, 1999)

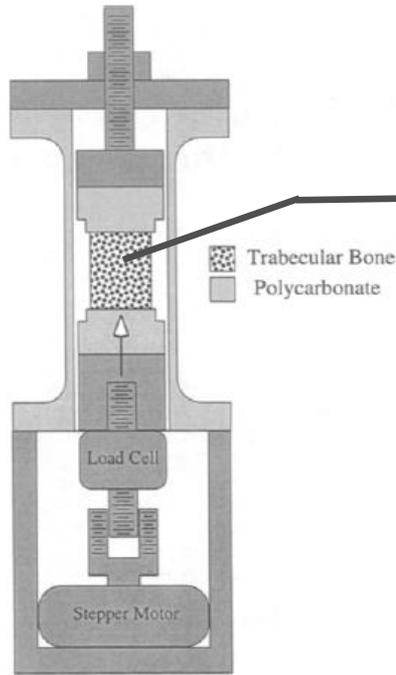
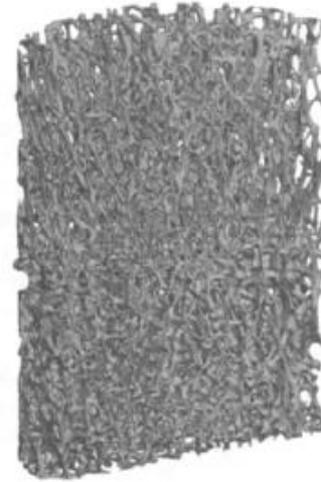
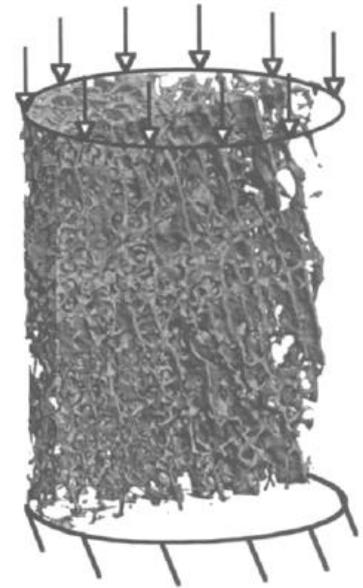


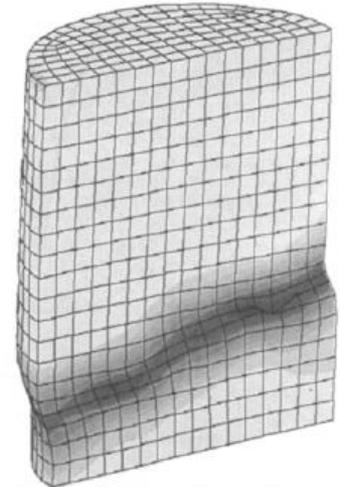
Fig. 1—The apparatus used for microCT scanning of trabecular bone samples under load



CT images of trabecular bone. Note the excellent contrast obtained throughout volume



Nominal Strain = 0.018  
Autoscaled



0.000 Min. Principal Strain -0.135





# 3D-DIC Applications

- **Heterogeneous material**
  - Woven glass-epoxy composite
  - Combined compression-bending loading
  - Large out-of-plane displacements
- Roofing Shingles
  - Background
  - Preliminary Experiments
  - Simulations





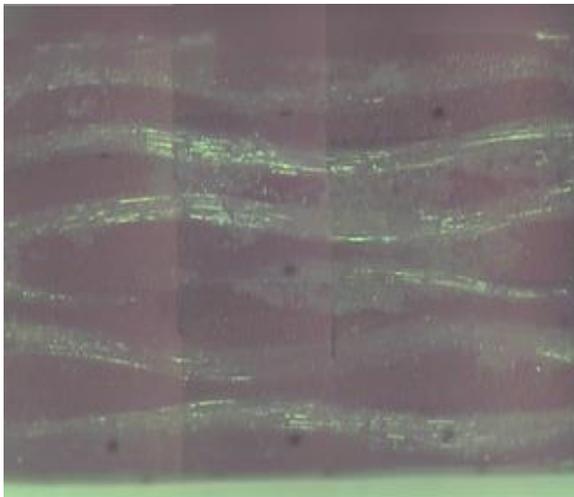
# Woven Glass-Epoxy Composite

## Material Specifics

- Thin sheet composite
- Glass-halogenated epoxy, NP-130
- Glass fibers approximately  $7\mu\text{m}$  diameter
- Five-six layers of orthogonally woven composite in plain weave structure for 1m by 1.3m sheets
- Rectangular specimens removed with razor knife



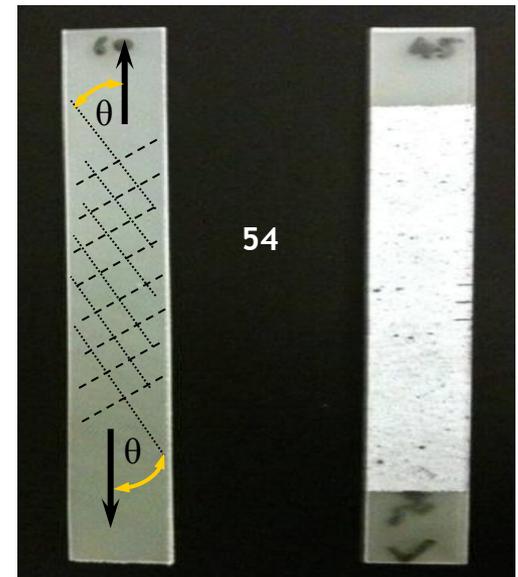
53



Edge View

## Specimen geometry

- TH: 1mm
- W: 17mm
- L: 150mm.



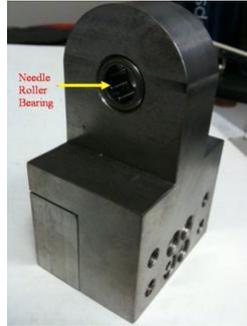
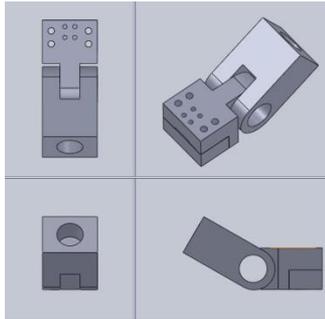
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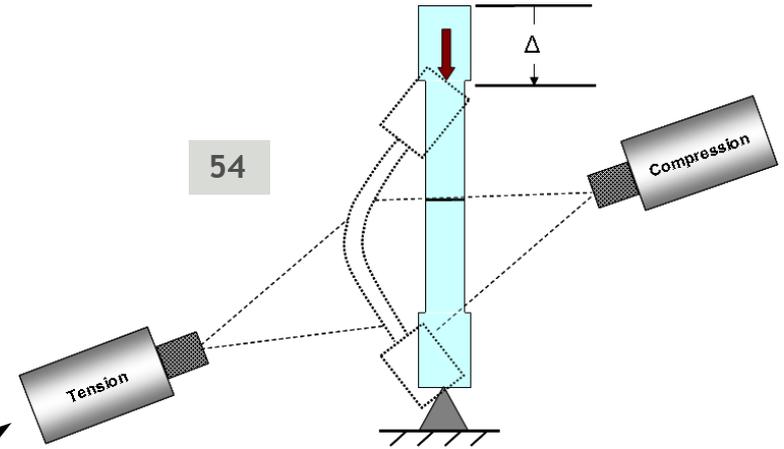


# Woven Glass-Epoxy Composite

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## System Schematic



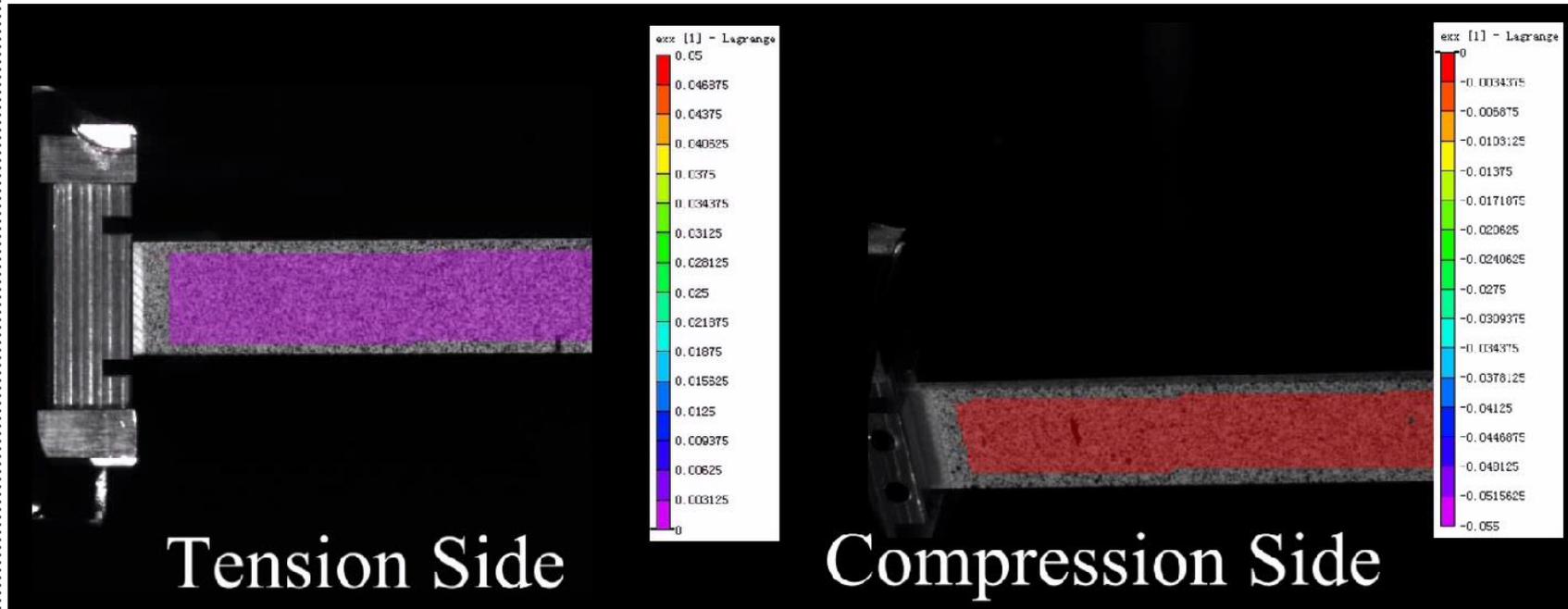
- Out-of-plane motions up to 40mm
- Compression side cameras
  - rotated counterclockwise by  $\approx 20^\circ$
  - moved closer to specimen
  - specimen at front of focus volume
- Tensile side cameras
  - rotated clockwise by  $\approx 20^\circ$
  - move away from specimen
  - specimen at back of focus volume





# Woven Glass-Epoxy Composite

Axial strain on compression and tension surfaces during combined compression-bending loading for  $\pm 45^\circ$  specimen.

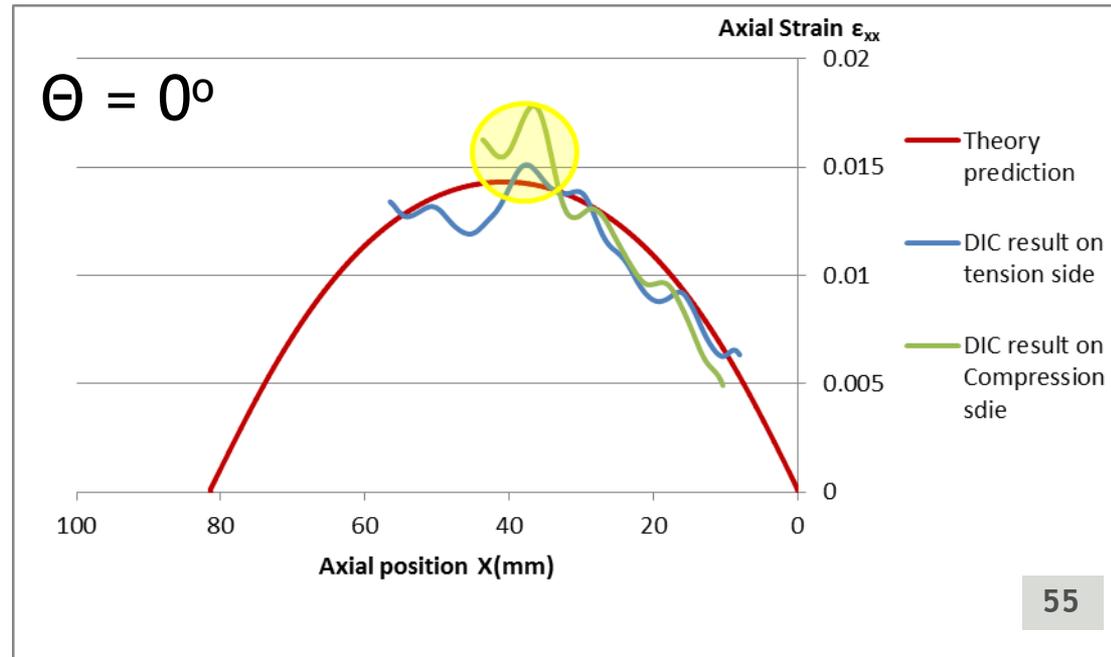


- Localized effects evident as  $w$  increases
- Critical regions have different spatial trends
  - Effect shown is muted for low fiber angles



# Woven Glass-Epoxy Composite

Axial strain for  $\Theta = 0^\circ$  and 20mm of axial displacement is in very good agreement with the large deformation results of the modified Drucker formulation on both surfaces.



55

*The elevated compressive strain in critical region appears to be due to localized damage, including fiber buckling and matrix failure.*





# Woven Glass-Epoxy Composite

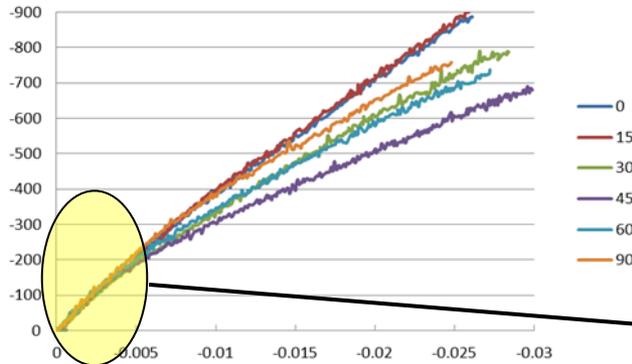
Effective stress vs effective strain in critical region near mid-span of specimen

$$\tilde{\epsilon}_\theta = \frac{\epsilon_\theta}{h(\theta)}, \quad \tilde{\sigma}_\theta = \sigma_\theta h(\theta)$$

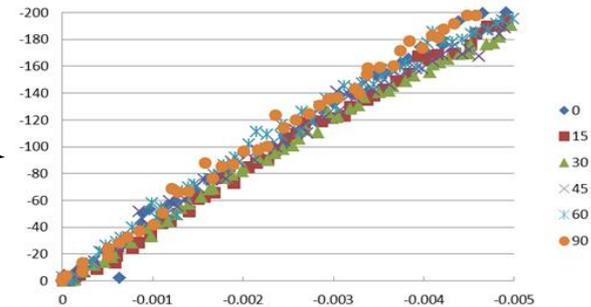
$$h(\theta) = \sqrt{\frac{3}{2} [\cos^4(\theta) + \frac{d_2}{d_1} \sin^4(\theta) + \frac{d_3}{d_1} \sin^2(\theta) \cos^2(\theta)]}$$

$$d_1 = \frac{1}{E_1}, \quad d_2 = \frac{1}{E_2}, \quad d_3 = \frac{1}{G_{12}} - \frac{2\nu_{12}}{E_1}$$

Effective Stress Vs Effective Strain on Compression Side

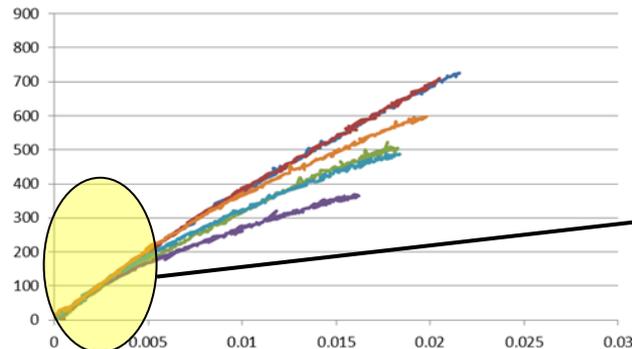


Effective Stress Vs Effective Strain on Compression Side



53

Effective Stress Vs Effective Strain on Tension Side



Effective Stress Vs Effective Strain on Tension Side

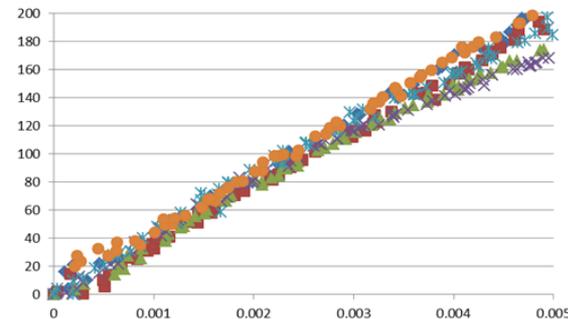


Figure 14



# Woven Glass-Epoxy Composite

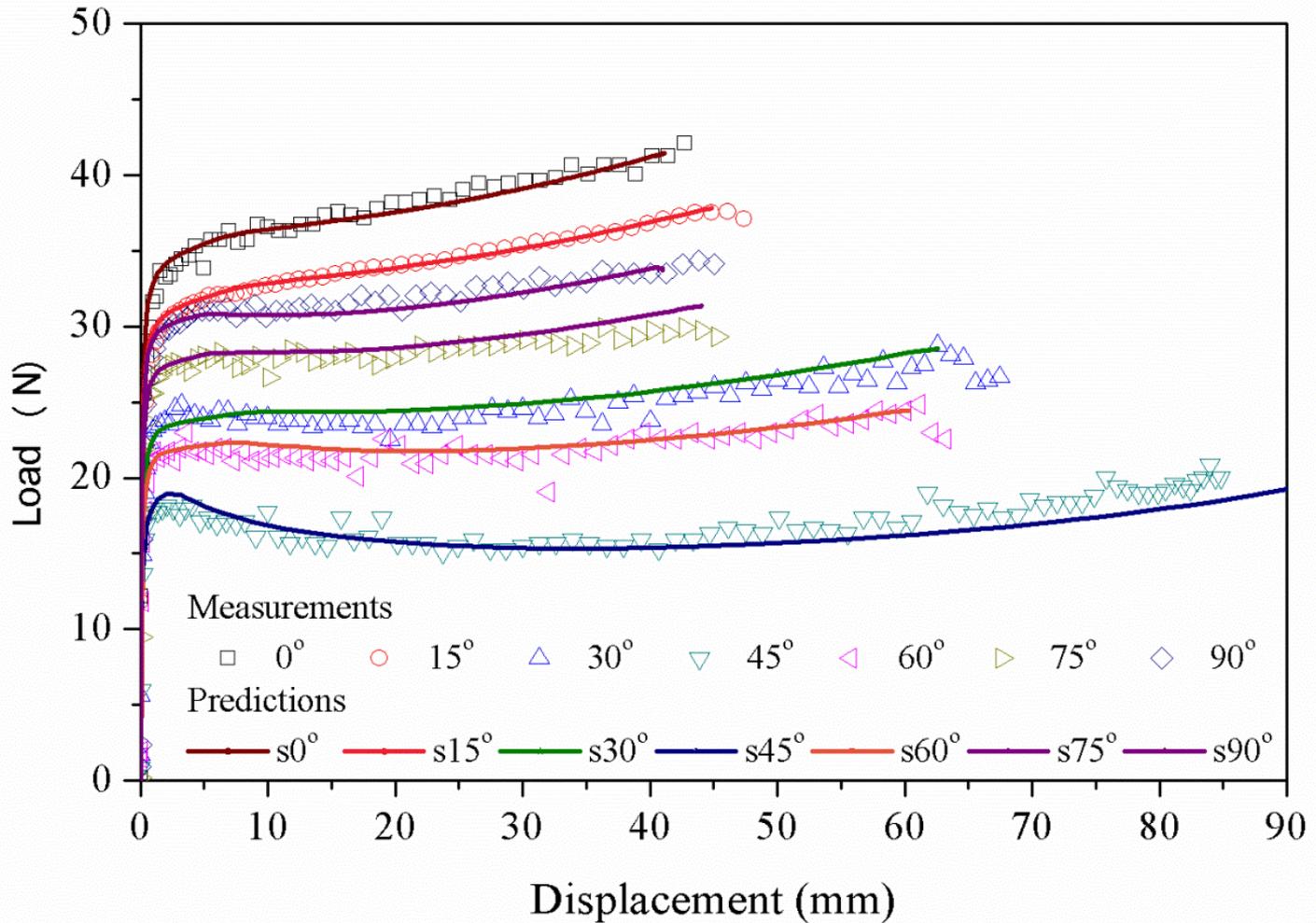


- **FE Simulations and Large Deformations**
  - Abaqus
  - Hashin damage model
  - 5 layers through total thickness-laminate construction modeled (not woven)
  - Alternating orthogonal fiber directions for layers (0-90-0-90-0) assumed
    - Layers modeled as individual orthotropic material (depending upon orientation of “fibers” relative to loading), with linear-elastic response and damage accumulation.
  - Hashin model parameters selected based on (a) literature data for glass-epoxy specimens of similar construction and (b) fitting of off-axis  $P-\delta$  response of bending-compression specimens.
    - Fibers are not modeled.





# Woven Glass-Epoxy Composite



- Differences between 15 and 75; 30 and 60 apparently due to CT-observed difference in fiber number in 0 and 90 orientations

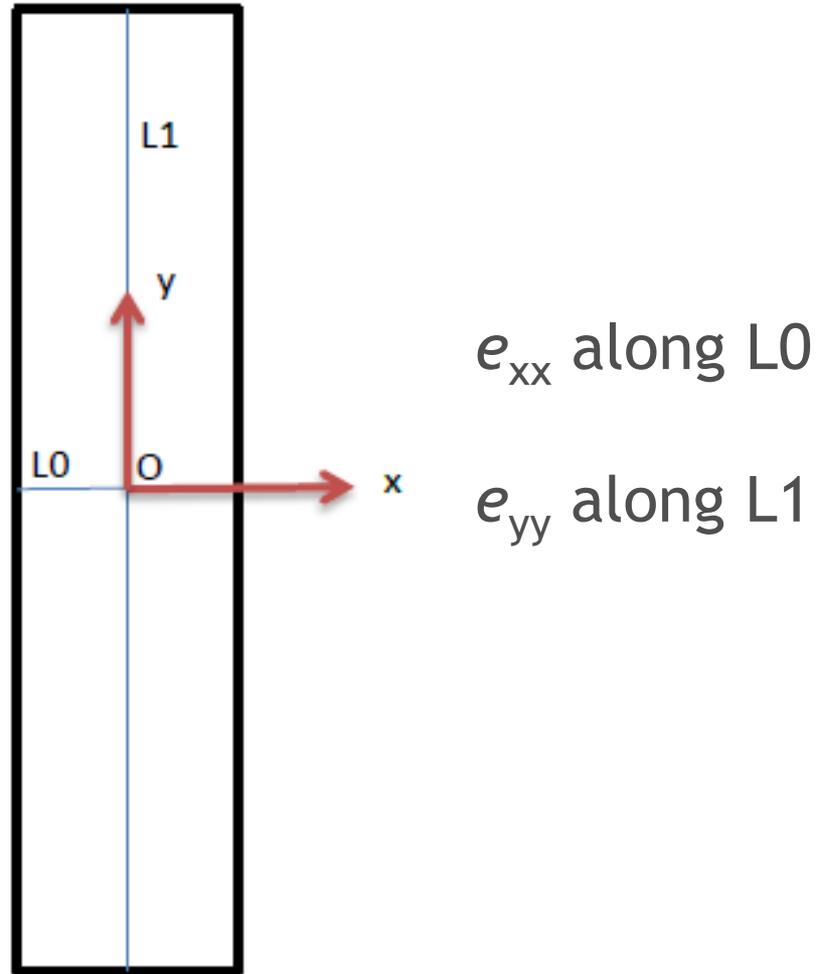




# Woven Glass-Epoxy Composite

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## Coordinate System



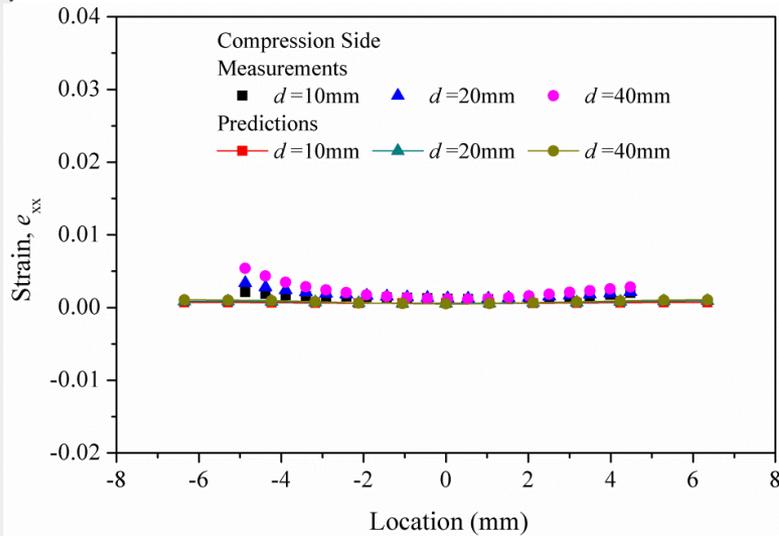
Front surface (compression side) of specimen



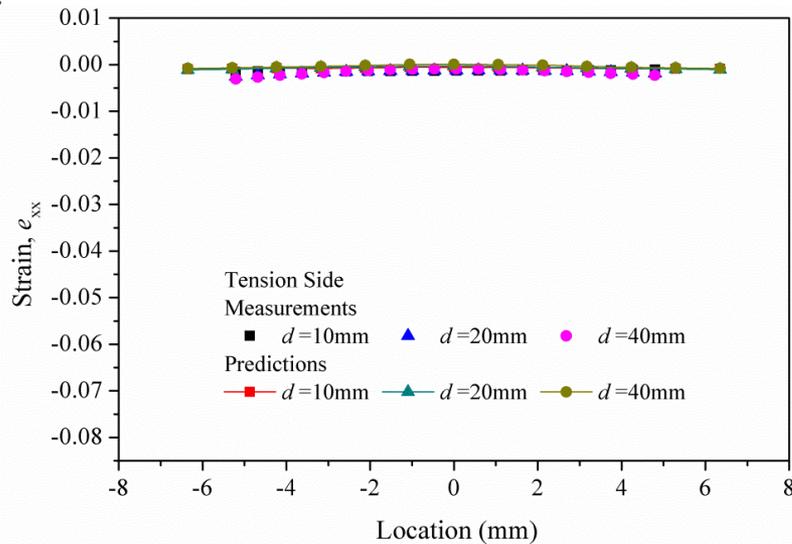
# Woven Glass-Epoxy Composite



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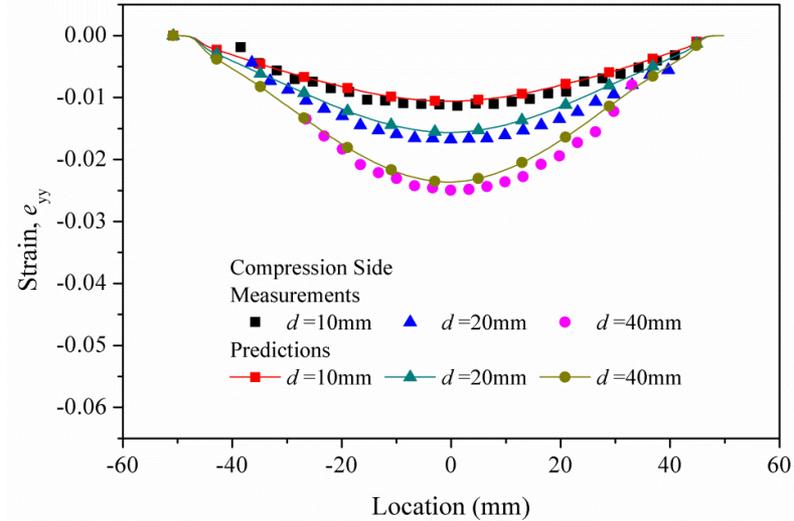


Compression side  $e_{xx}$

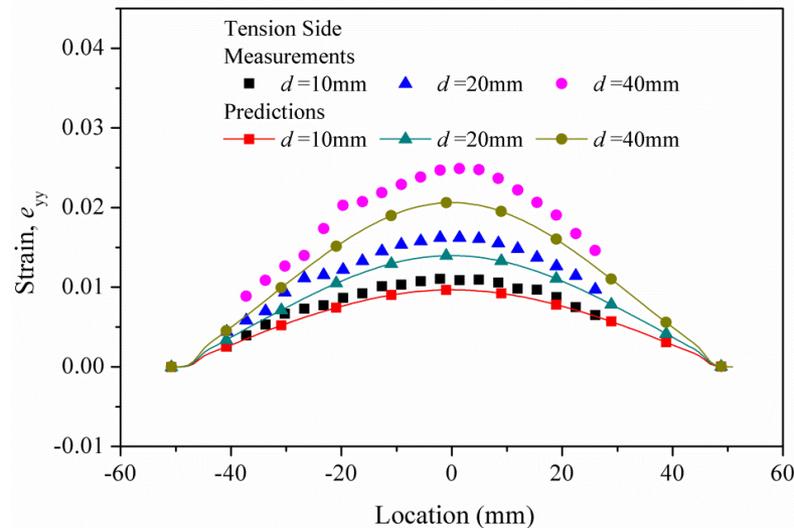


Tension side  $e_{xx}$

$0^\circ$



Compression side  $e_{yy}$



Tension side  $e_{yy}$



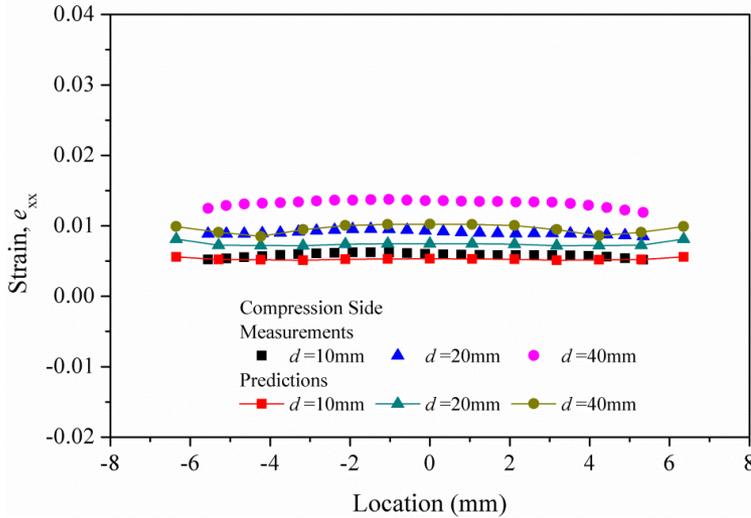
# Woven Glass-Epoxy Composite



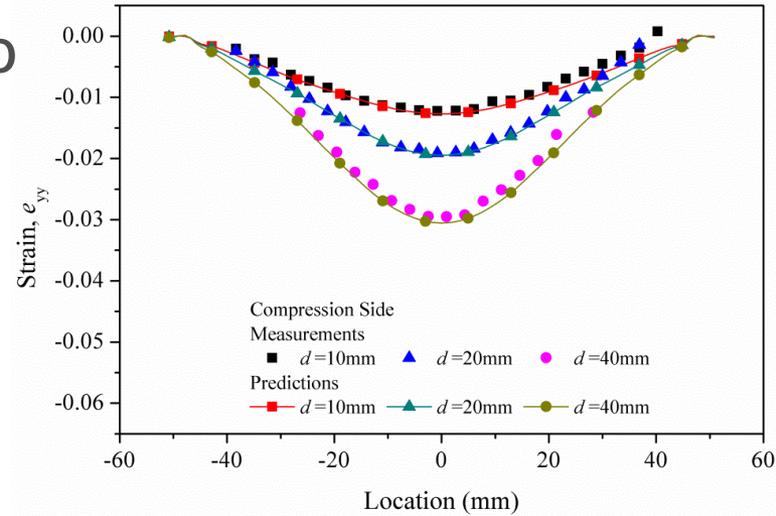
University of South Carolina



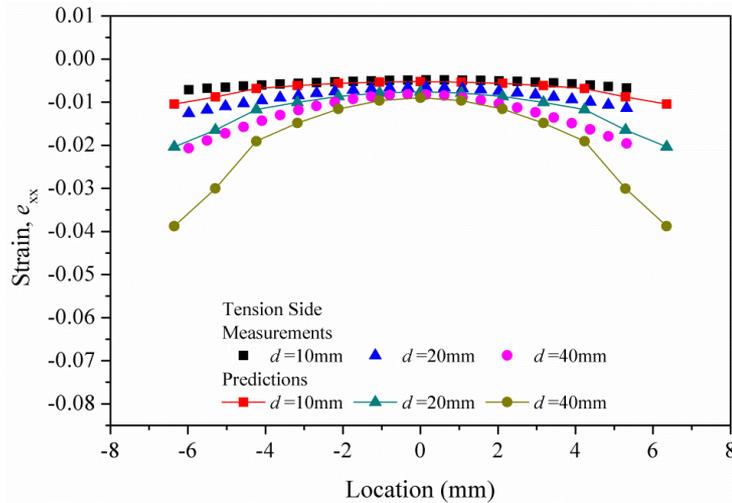
60°



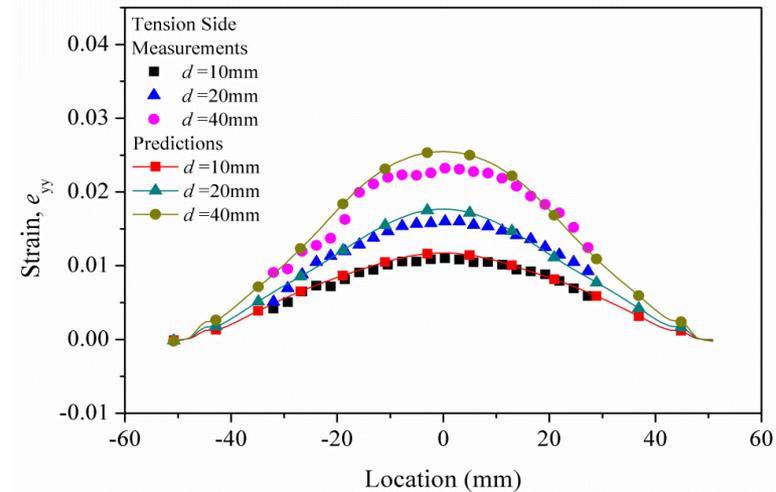
Compression side  $e_{xx}$



Compression side  $e_{yy}$



Tension side  $e_{xx}$



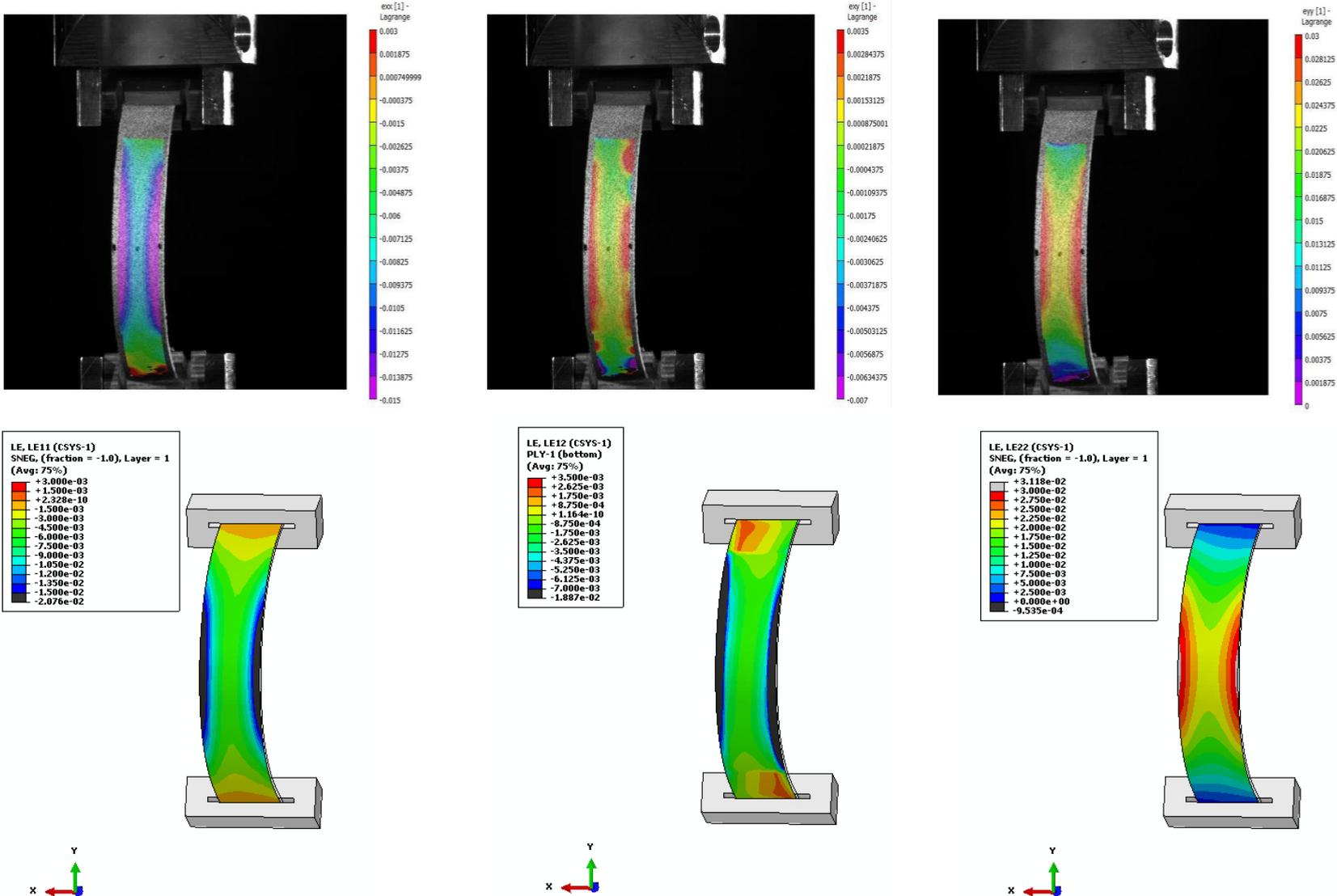
Tension side  $e_{yy}$

# Woven Glass-Epoxy Composite

60° at D = 40 mm, Tension side



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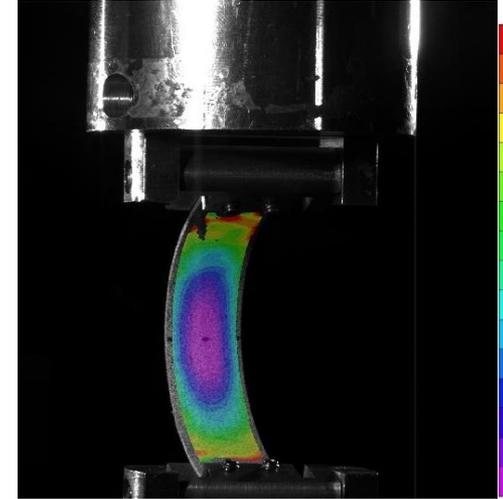
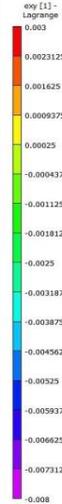
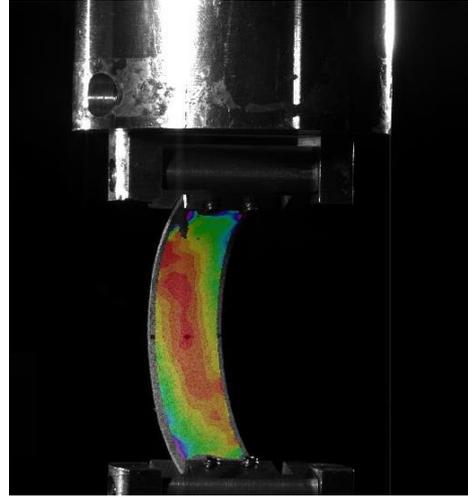
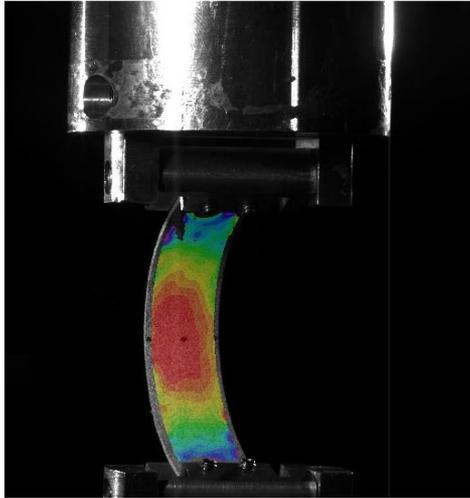


# Woven Glass-Epoxy Composite

60° at D = 40 mm, Compression side

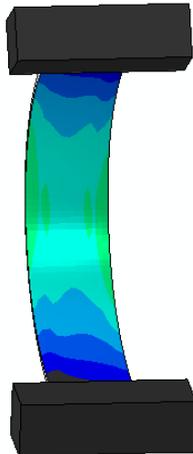


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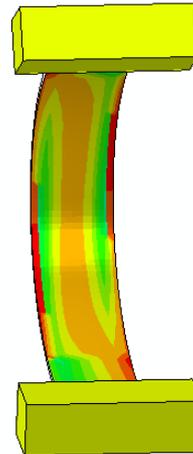
LE, LE11 (CSYS-1)  
SPDS, (fraction = 1.0), Layer = 12  
(Avg: 75%)

+	1.500e-02
+	1.392e-02
+	1.283e-02
+	1.175e-02
+	1.067e-02
+	9.585e-03
+	8.500e-03
+	7.417e-03
+	6.333e-03
+	5.250e-03
+	4.167e-03
+	3.083e-03
+	2.000e-03
-	4.182e-04



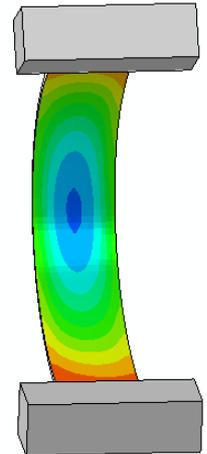
LE, LE12 (CSYS-1)  
SPDS, (fraction = 1.0), Layer = 12  
(Avg: 75%)

+	3.000e-03
+	2.083e-03
+	1.167e-03
+	5.500e-04
+	6.667e-04
-	1.383e-03
-	2.500e-03
-	3.417e-03
-	4.333e-03
-	5.250e-03
-	6.167e-03
-	7.083e-03
-	8.000e-03



LE, LE22 (CSYS-1)  
SPDS, (fraction = 1.0), Layer = 12  
(Avg: 75%)

+	8.263e-04
-	3.000e-03
-	5.250e-03
-	7.500e-03
-	9.750e-03
-	1.200e-02
-	1.425e-02
-	1.650e-02
-	1.875e-02
-	2.100e-02
-	2.325e-02
-	2.550e-02
-	2.775e-02
-	3.000e-02





# Applications

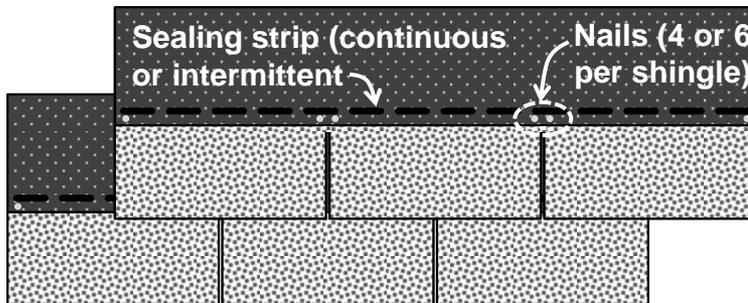
- Heterogeneous material
  - Woven glass-epoxy composite
  - Combined compression-bending loading
  - Large out-of-plane displacements
- **Roofing Shingles**
  - Background
  - Preliminary Experiments
  - Simulations





# Roofing Shingles

- Roof asphalt shingles
  - The most common type of sloped-roof cover for residential construction in the US
  - Shingles consist of:  
Two layers of asphalt, fiberglass mat and granules
  - Sealing strip (introduced in the 1950s):
    - ✓ Minimizes the water penetration
    - ✓ Resists against wind-induced uplift

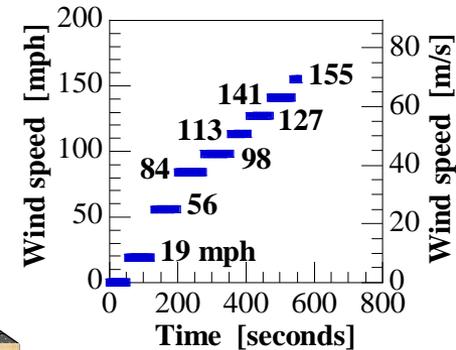
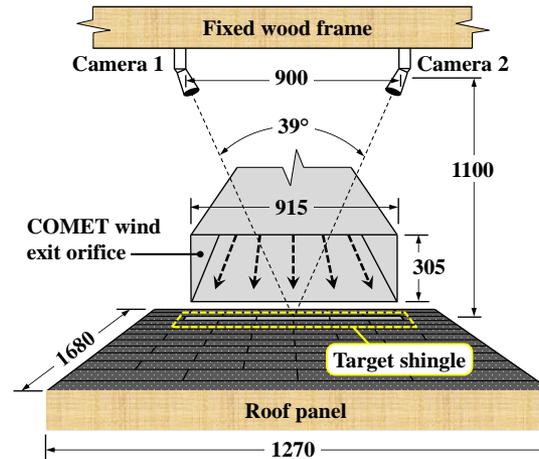
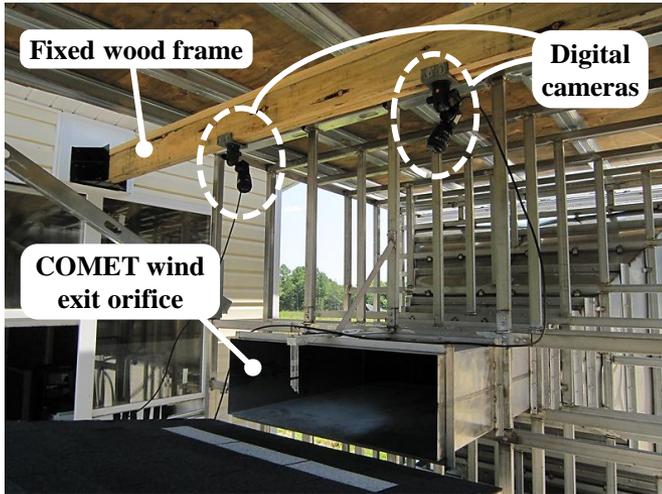




# Roofing Shingles

## Experimental Program

### ➤ 3D-DIC setup and wind load



- Cannot paint surface due to stiffening effect on soft shingle material
- Cameras: Two 5 MP (Point Grey Grasshopper GRAS-50S5M-C)
- Lenses: 28-mm lenses (AF Nikkor 28 mm f/2.8D)
- Cameras were mounted on a fixed wood frame to minimize wind-induced vibrations
- Roof cover was built to minimize changes in ambient light
- 5 Hz frequency was used to acquire and store thousands of images





# Roofing Shingles

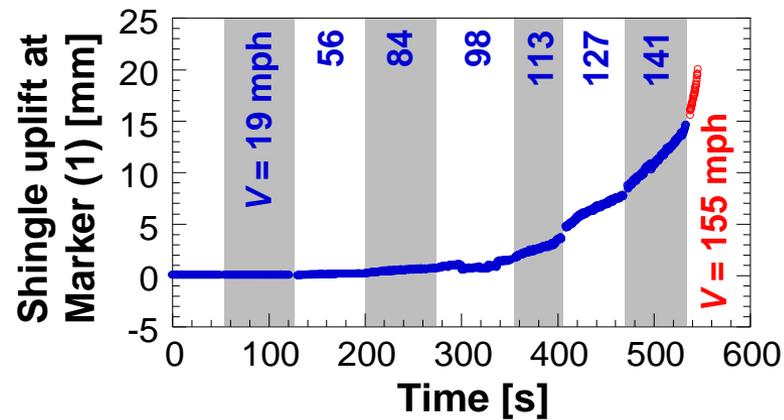
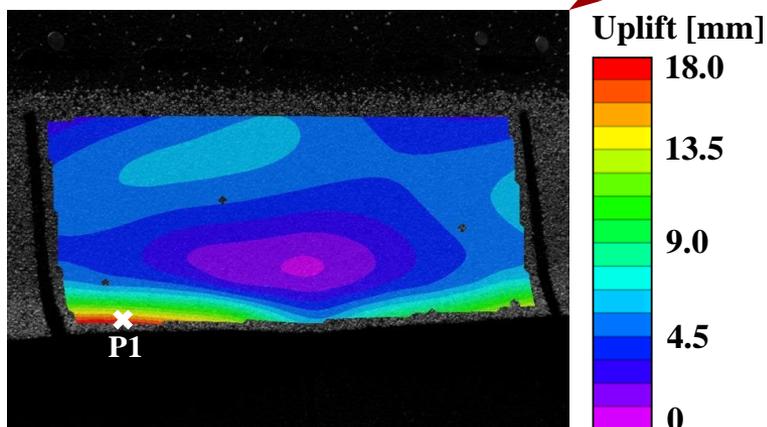
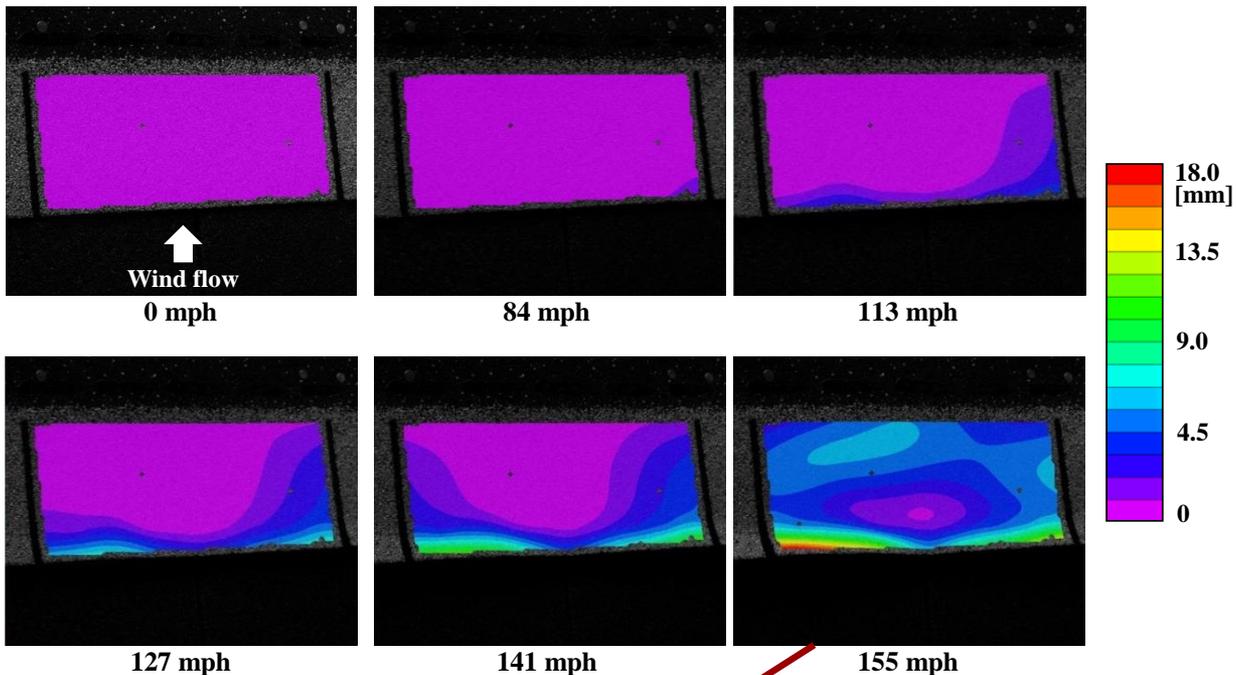
- 340kmph wind. Time sped up by 10X.
- Audio turned off due to high dB noise.





# Roofing Shingles

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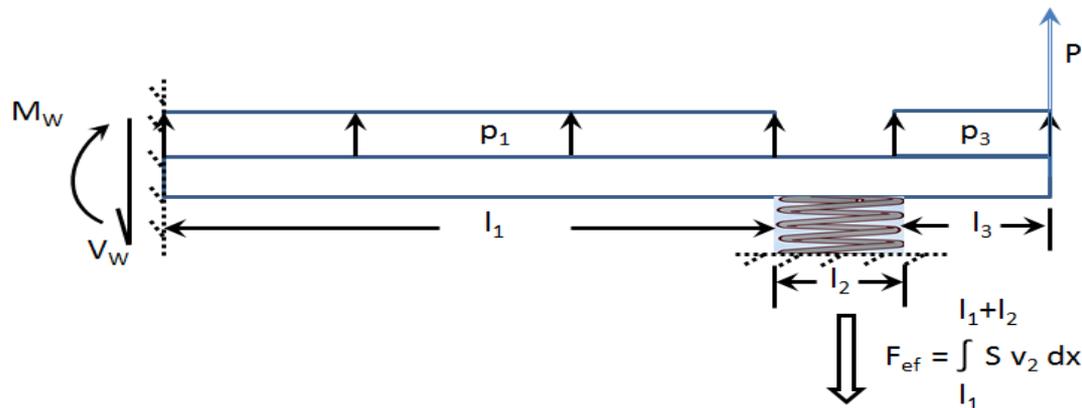




# Roofing Shingles

## Simulation of Shingle Response and Sealant Separation

- Beam on elastic foundation (BOEF) model is employed with finite sealant
  - “Foundation” represents effect of sealant material
  - Assume elastic response throughout deformation process. Beam and sealant lengths and properties obtained experimentally from commercially available shingle samples.
  - Uplift pressure  $p_1$  measured independently for winds up to 200km/hr
  - Energy release rate at each edge of sealant strip is  $\frac{1}{2} S v_2^2$
  - Drag force,  $P$ , not included in these results
  - Solution requires determination of 12 parameters

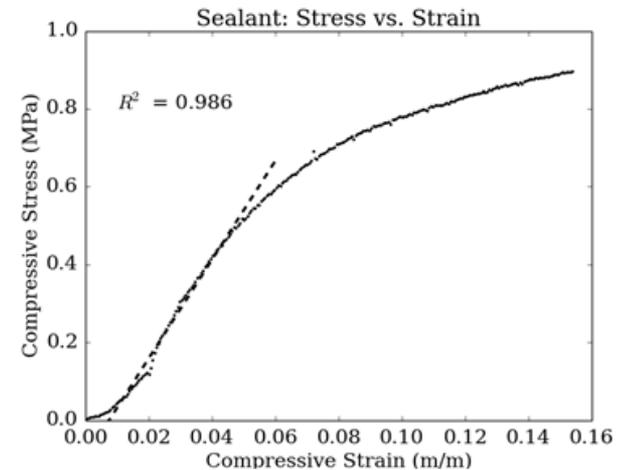
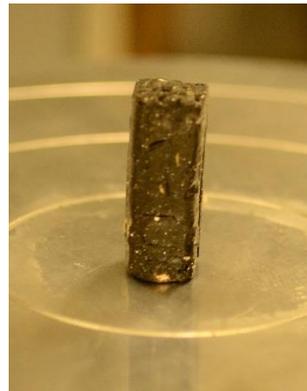
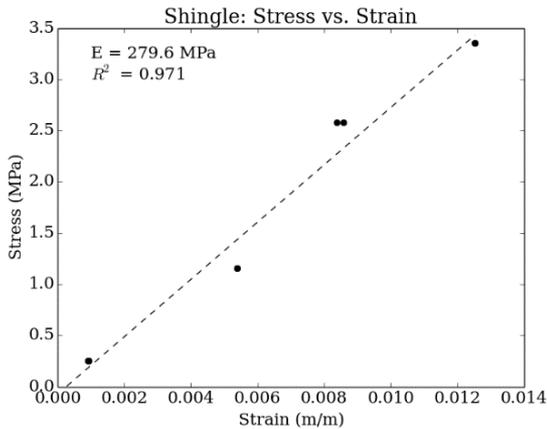
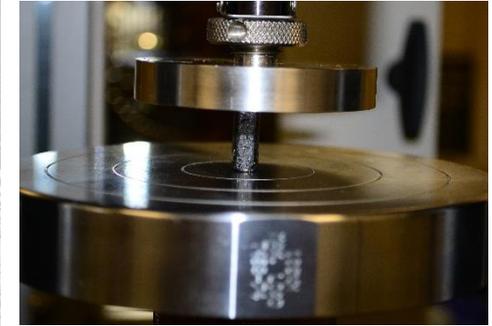
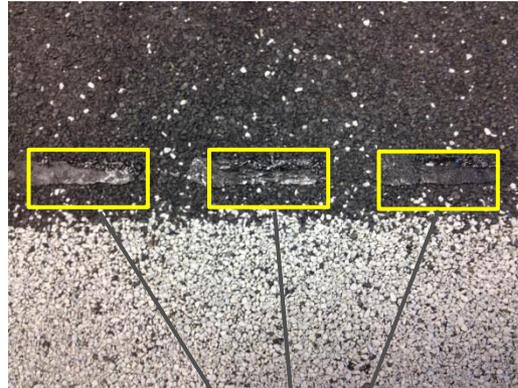
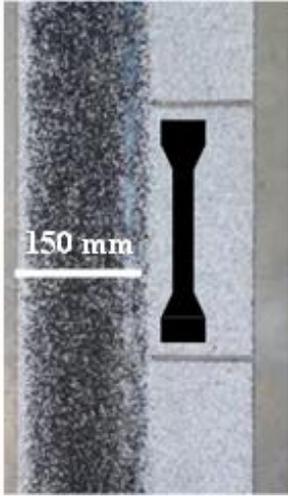




# Roofing Shingles

## Preliminary Experiments

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Shingle length,  $0 \leq l_1 \leq 0.1204 \text{ m}$

Sealant length,  $l_2 = 0.0127 \text{ m}$

Overhang length,  $l_3 = 0.0254 \text{ m}$

Sealant thickness:  $t = 2.8 \text{ mm}$

BOEF Sealant Parameter:  $S = 4.53 \text{ Gpa m}^{-1}$

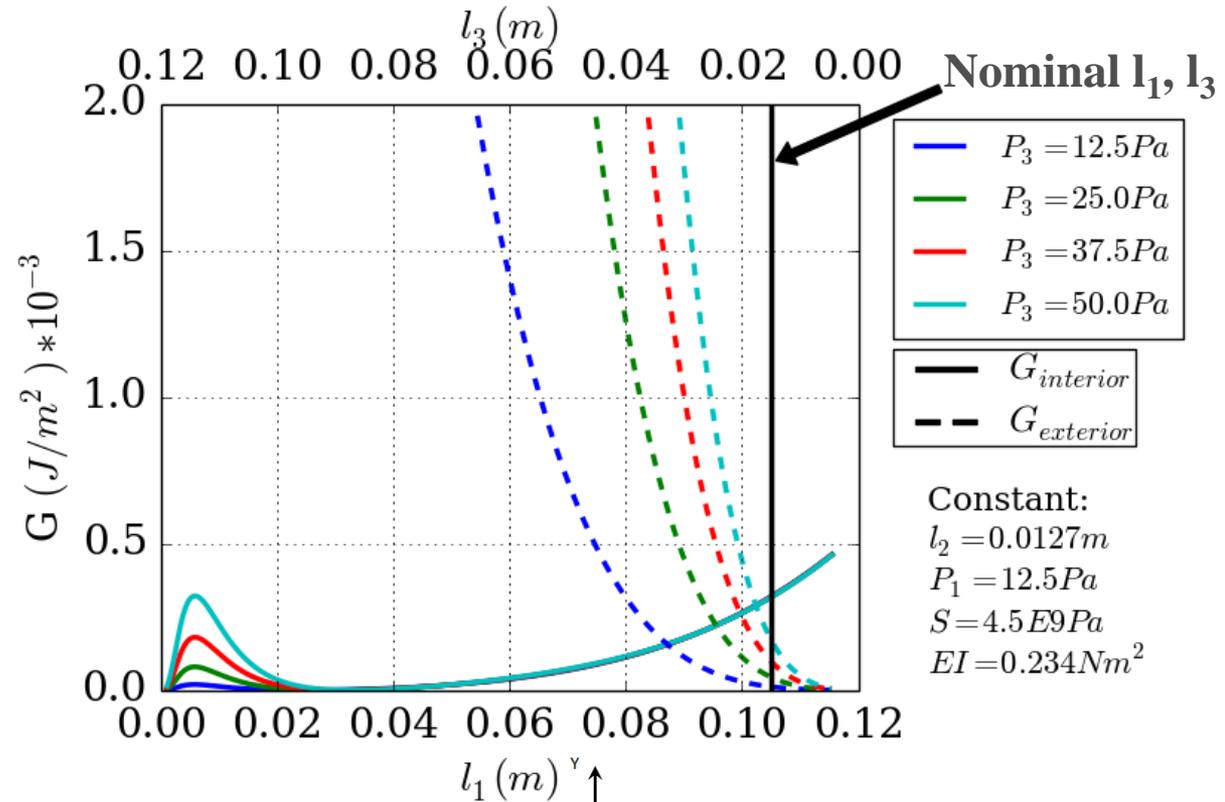
Compressive axial stress vs. axial strain measurements for sealant specimen at 23°C.



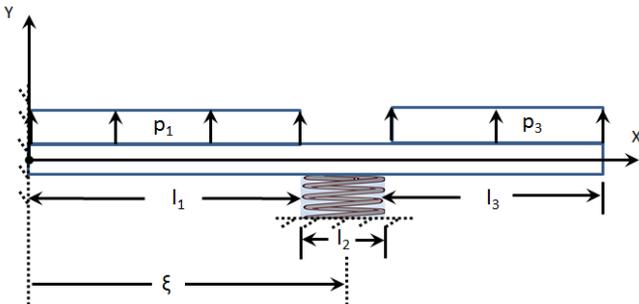


# Roofing Shingles

## Simulation Results-Energy Release Rate



Applied  $q$  at the interior and exterior **edges** of sealant as function of sealant location,  $\xi$ , with constant sealant and overall beam lengths. Solid lines represent  $q$  at interior sealant edge and dashed lines represent  $q$  at external sealant edge for different pressures.





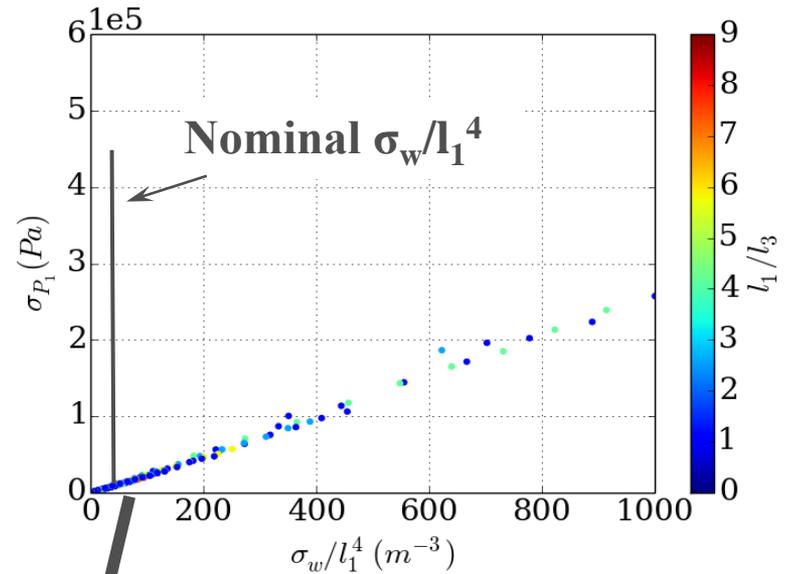
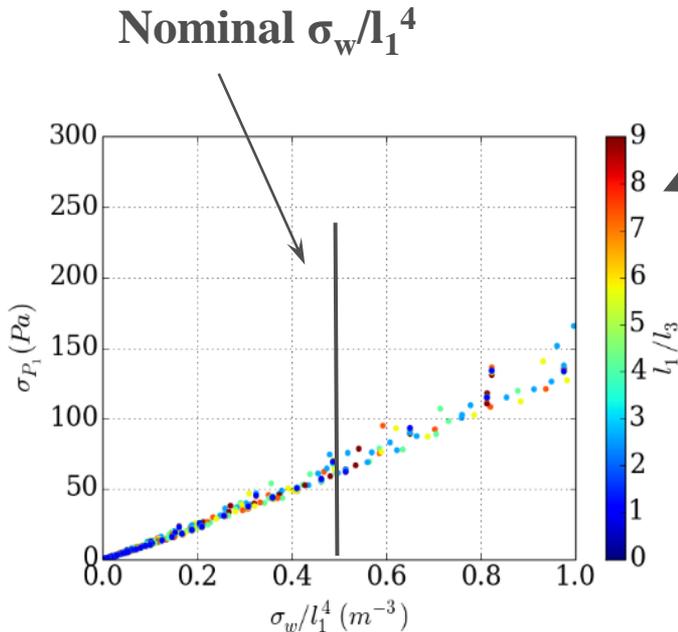
# Roofing Shingles

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## Simulations to Assess Potential to Quantify Pressures Using 3D-DIC

$\sigma_w$  = variability in 3D-DIC measurements = 50 $\mu\text{m}$

$\sigma_{P_1}$  = variability in applied pressure



Since  $P_1 = 12.5\text{Pa}$ , for nominal geometry the standard deviation for a single measurement is nearly 60Pa. Thus, one must take nearly 1800 image pairs to obtain variability of 1.25Pa in the predicted pressure....





# Concluding Remarks

- The rapid growth of computer hardware speed since mid-1990s has resulted in both the expansion of computational methods and the explosive growth of digitally-based experimental methods.
- Digital image correlation methods provide a platform for the recording large quantities of full-field deformation data under a broad range of conditions
  - High rate loading (cameras can record images every 5 nanoseconds)
  - High temperature (cameras can acquire usable images for DIC on specimens where  $T > 1200^{\circ}\text{C}$ )
  - Small (down to  $20\mu\text{m} \times 20\mu\text{m}$ ) and large (full-scale aircraft) regions can be measured.
  - Long term studies (experiments lasting several days or longer) have been reported.
- The combination of full-field measurements with theoretical and computational models provides a rich framework for improving our understanding of the physical world.





# The Future

*“The future of science is neither vague nor unimaginable.  
It is the result of what we do now.”*

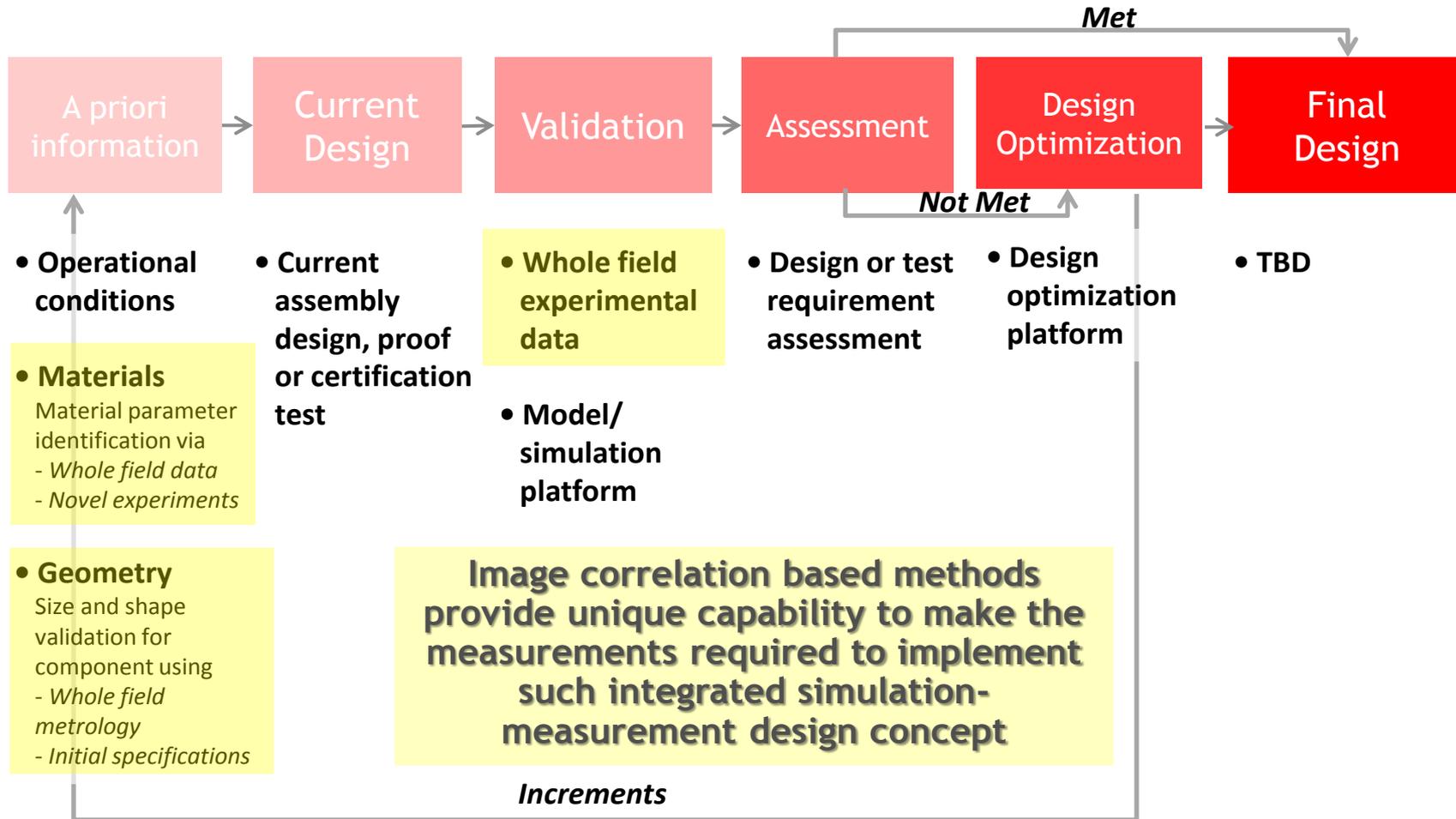
- Integration with Design and Development
  - Data-driven simulations for design
- Future Trends in Digital Image Based Methods
  - Multiple measurement system integration
  - Continued growth of data-driven parameter estimation approaches
  - Full integration of analysis and measurements for multi-physics studies





# Integration with Design and Development

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# Integration with Design and Development

- The ability to smoothly integrate full-field measurements using 2D-DIC, 3D-DIC and/or V-DIC with design simulations requires efficient and robust optimization methodologies that can effectively identify the constrained optimal combination of
  - Material parameters
  - Structural configurations
  - Operational conditions
- Successful implementation of DIC-based measurement methods with simulation platforms offers opportunities to replace existing “testing standards” with a far more robust design methodology
- Education level of the next generation of designers must be adequate for this approach to be viable.





# Future Trends in Digital Image Based Methods

## Integration of multiple measurement systems

- *Synchronized measurements with multiple measurement technologies*
  - CT systems for slow speed events
  - Stereovision systems
    - Slow speed events
    - High speed events
  - Thermographic camera systems
  - Multiple average or local sensor measurements
    - Pressure
    - Loads
    - Moments
    - Voltage
    - Current
    - Other environmental variables

▫





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*Dr. Robert S. Piascik*

*Dr. Stephen W. Smith*



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*Dr. David Stargel*



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*Dr. Philip Reu*

*Dr. Timothy Miller*





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# Future Trends in Digital Image Based Methods

- *Continued expansion of parameter identification*

- Common optimization metric;

$$\mathbf{E} = \sum_i \sum_j (F(\underline{x}_i, t_j; \mathbf{B}), - f(\underline{x}_i, t_j) )^2$$

$F()$  = theoretical function for measurable quantity

$f()$  = experimental measurements for quantity

$\underline{x}_i$  =  $i^{\text{th}}$  spatial position on specimen

$t_j$  =  $j^{\text{th}}$  time of interest

$\mathbf{B}$  = vector of unknown parameters by minimizing  $\mathbf{E}$

*Examples: mixed mode stress intensity factors using full-field crack tip data, composite material parameters*





# Future Trends in Digital Image Based Methods

- *Full integration of analysis and measurements for multi-physics studies*
  - Experimental measurements combined with multi-physics models coupling effects from multiple environmental factors.
    - Multi-physics model validation using estimated parameters
    - Model employed for predictions in regimes where experimental measurements are more difficult

“The future? It is impossible to envision the unimaginable, and wonderful to see it happen.”





# Future Trends in Digital Image Based Methods

University of South Carolina

## Recent DIC-Related Activities

- Article in Applied Mechanics Reviews (6/2013)
- Special issue in Experimental Mechanics focusing on Digital Image Correlation (1/2015)
- 2<sup>nd</sup> edition of book is under development, highlighting the most recent trends in DIC and applications





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# Brief History: Measurement Methods

- Issues associated with extraction of deformation information using film as a recording media
  - Non-linearity in film
  - Film processing (*darkroom*)
  - Film stability and handling
  - Laser illumination
  - De-correlation effects (*previous slide*)
  - Exorbitant time requirements
  - Inaccuracies in reconstruction process
    - fringe location
    - film expansion/contraction
    - relationship of object to image coordinates
    - distortions in imaging process

